

# Analytical ultracentrifugation

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# Outline

- AUC background
- How AUC experiments are performed
- Data analysis
- Example: simple model-independent investigation of a hetero-association
- Detergent solubilised systems
- Hydrodynamic bead modelling (HBM)
- Example: oligomerisation of synthetic polyvalent integrin  $\alpha_5\beta_1$  ligands

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# AUC tutorials

- Setting up and running AUC experiments
  - Tutorial paper
    - Lebowitz, J., M.S. Lewis, and P. Schuck, Modern analytical ultracentrifugation in protein science: A tutorial review. Protein Science, 2002. 11(9): p. 2067-2079.
  - AUC user guide from Demeler lab
    - <http://www.uslims.uthscsa.edu/AUCUserGuideVolume-1-Hardware.pdf>
- Data analysis
  - Using SEDFIT & SEDPHAT
    - <http://www.analyticalultracentrifugation.com/default.htm>
  - Using Ultrascan
    - <http://www.ultrascan.uthscsa.edu/>



# Questions that can be answered by AUC

- Is sample heterogeneous?
  - If yes, is it in molecular weight, shape, or both?
  - If yes, does it depend on pH, salt, buffer, etc?
- Is sample pure enough for X-ray crystallography, SAXS, SANS or NMR?
- Does sample...
  - ...self-associate?
  - ...aggregate?
- What is molecular weight of sample, or a mixture of samples?
- Does sample bind to a ligand?
- What is stoichiometry of binding?
- What is  $K_d$ ?
- Is association state/conformation affected by tagging?

# More questions that can be answered by AUC

- What is sedimentation & diffusion coefficient?
  - Globular or unfolded/disordered?
  - Is conformation dependent on salt, pH, ligand concentration, deuteration, etc?
- Do mutations affect  $K_d$ , conformation, stoichiometry, etc?
- Is sample affected by crowding?

# The analytical ultracentrifuge (AUC) was invented by Theodor (The) Svedberg

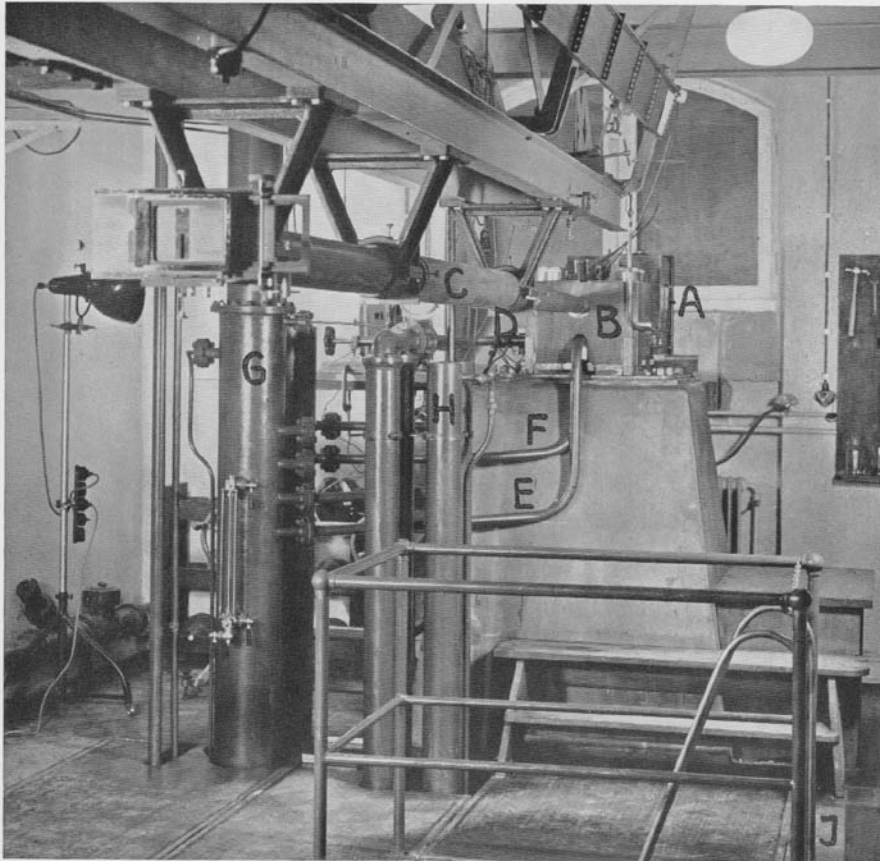


FIG. 68. Oil-turbine ultracentrifuge laboratory at Upsala

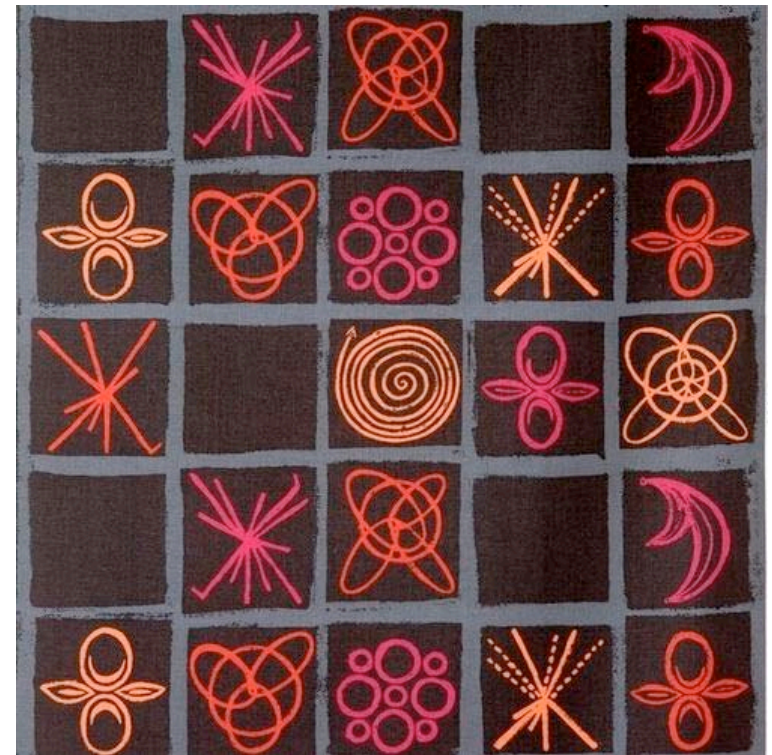
- |                        |                                      |
|------------------------|--------------------------------------|
| A. Lamp-house;         | F. Bearing oil outlet and oil drain; |
| B. Centrifuge;         | G. Main oil container;               |
| C. Camera;             | H. Oil coolers;                      |
| D. Turbine oil inlet;  | I. Steps to compressor pit.          |
| E. Turbine oil outlet; |                                      |



Nobel Prize in Chemistry 1926 awarded to The Svedberg *"for his work on disperse systems"*

# Svedberg was an interesting man...

- Married 4 times
- 12 children!
- Liked to paint
  - “Atomics”



*Svedberg in front of his textile print Atomics. (Gustaf Werner Institute archives)*

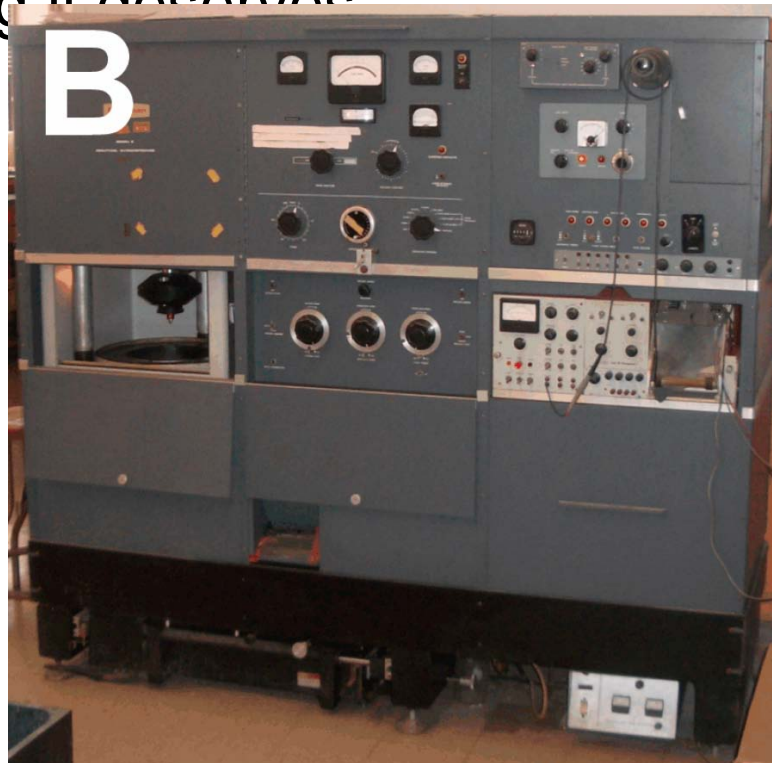


*Svedberg in front of his textile print Atomics. (Gustaf Werner Institute archives)*

# 1960's-80's

## AUC = core biochemical/biophysical technology

- Advice from the Beckman Model E AUC 1964 manual:
- “The Model E, like a woman, performs best when you care. But you needn't pamper it - just give it the understanding it deserves.”



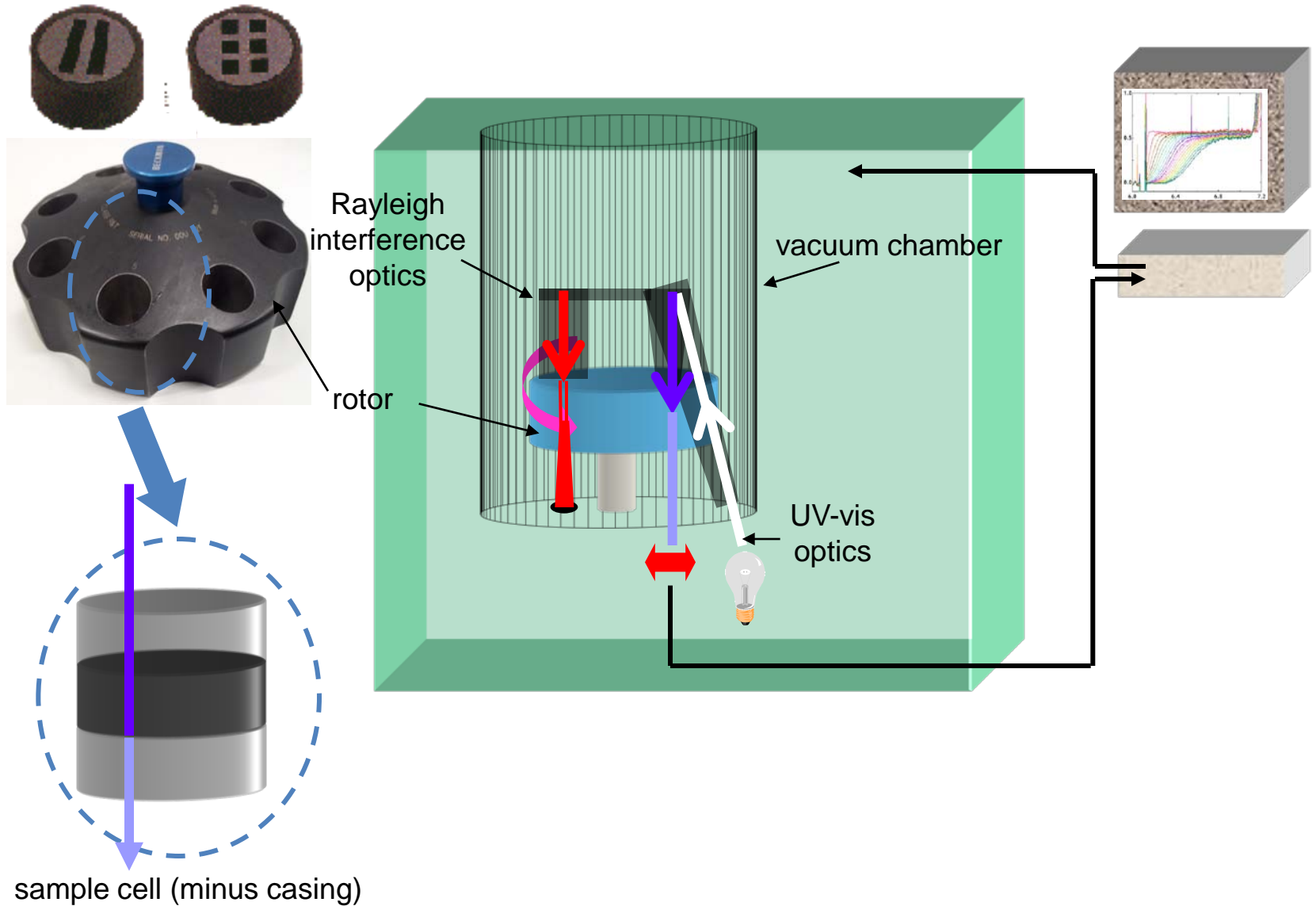


# The modern AUC a high speed preparative UC with optics



Beckman Coulter ProteomeLab XL-A/XL-I; €250-350 k

# Inside the Beckman Coulter XL-I





# Relationship between data and sample: absorbance

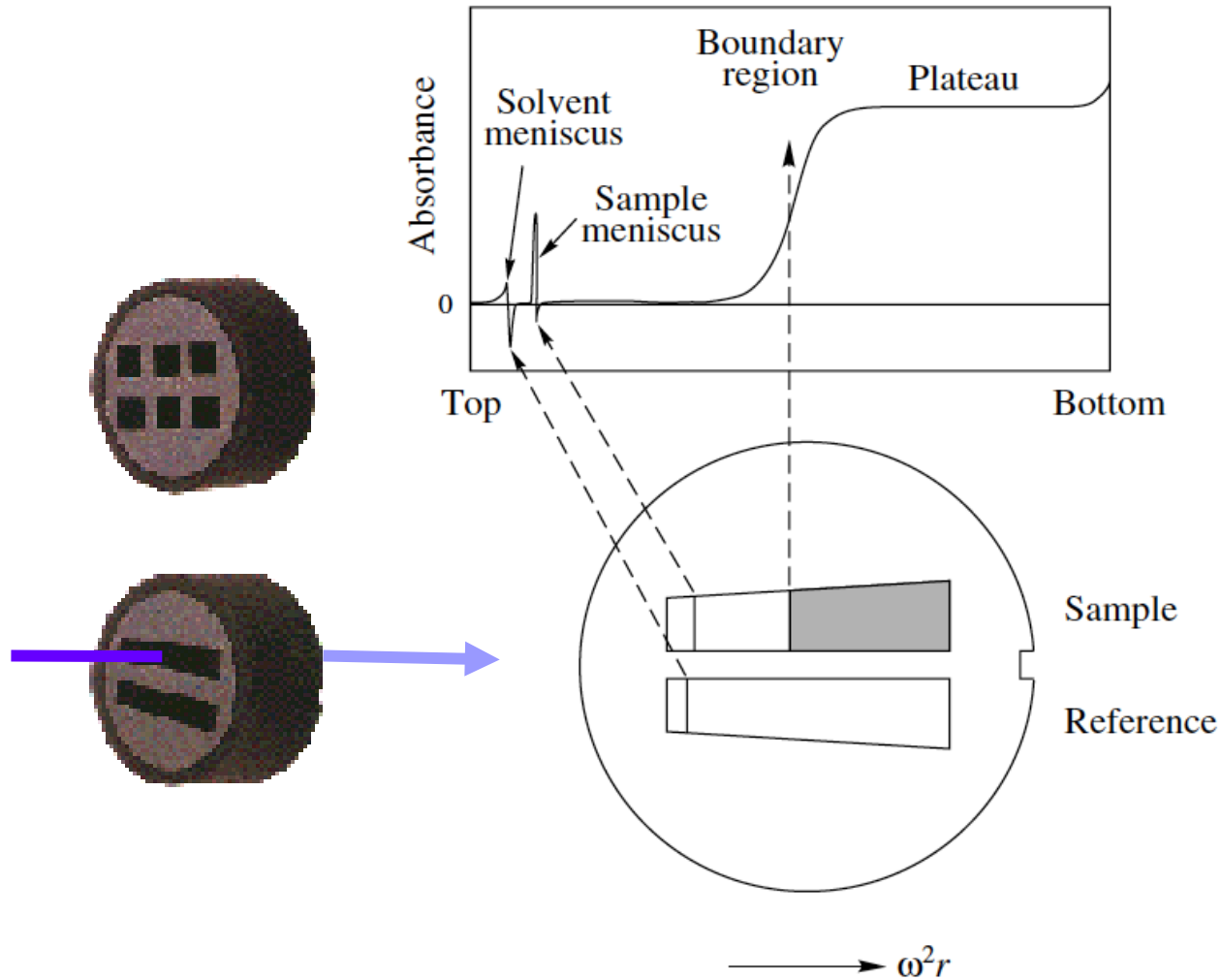
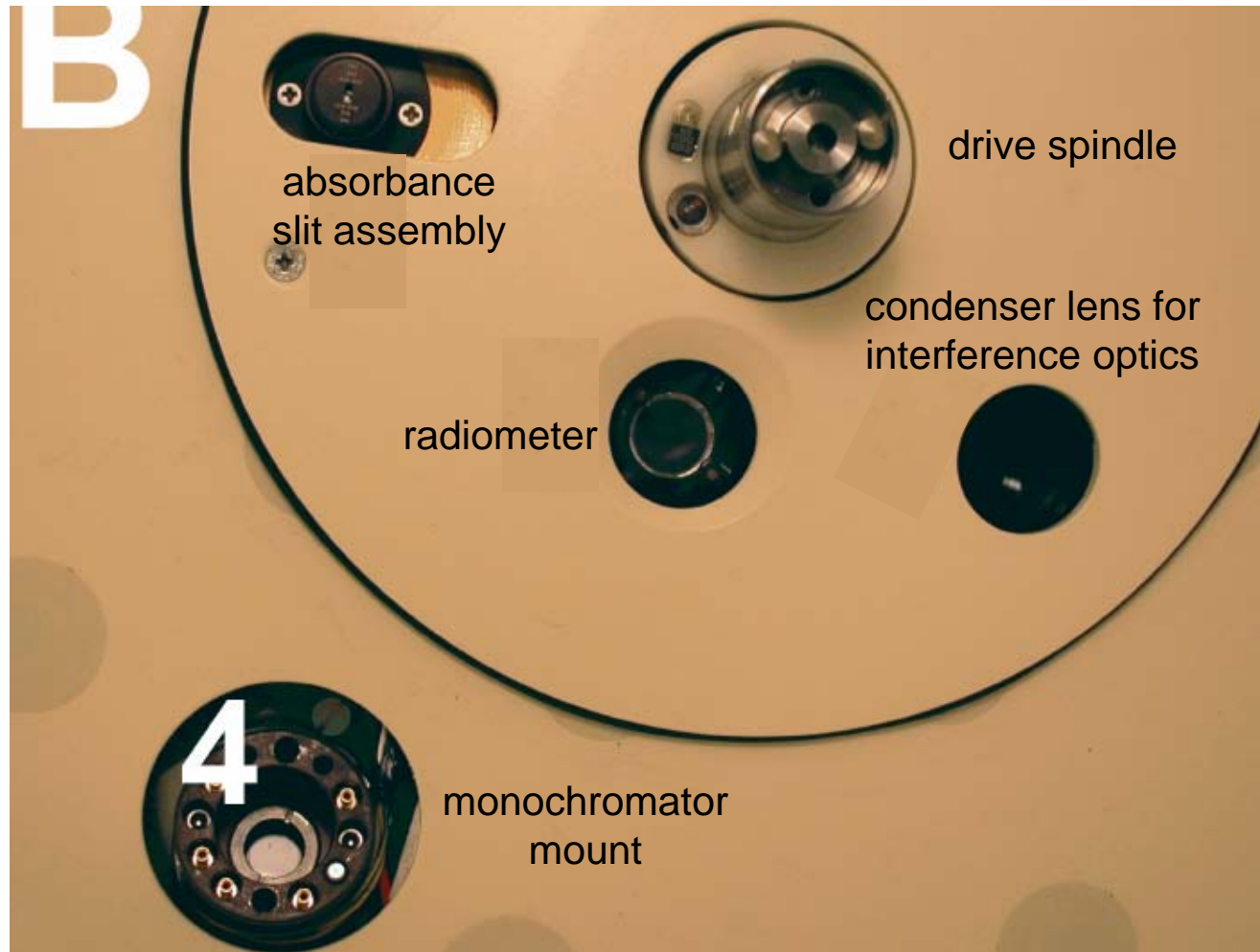


image from Ralston, 1993

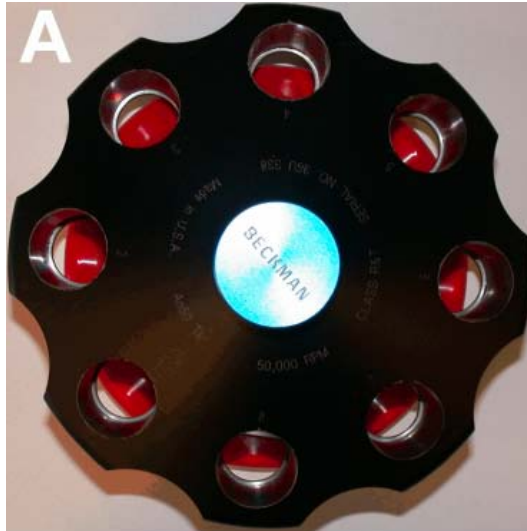
<https://www.beckmancoulter.com/wsrportal/bibliography?docname=361847.pdf>

# Inside the rotor chamber

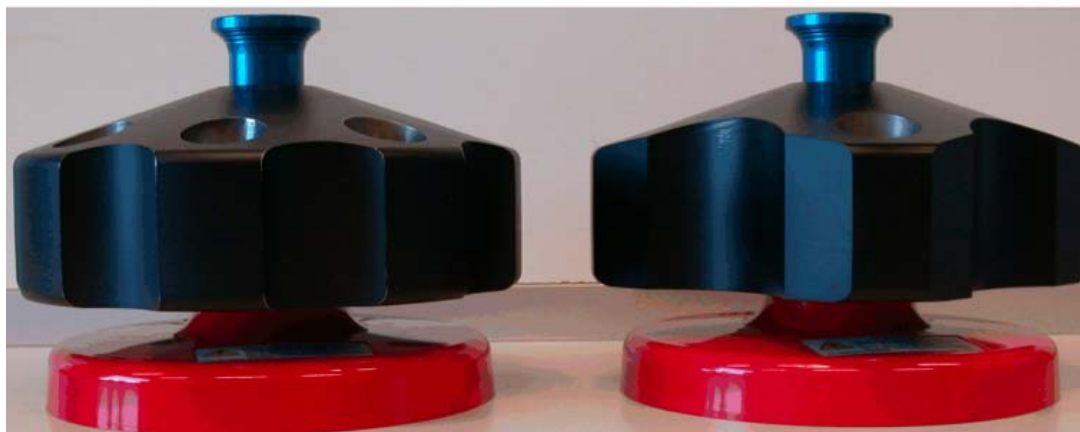
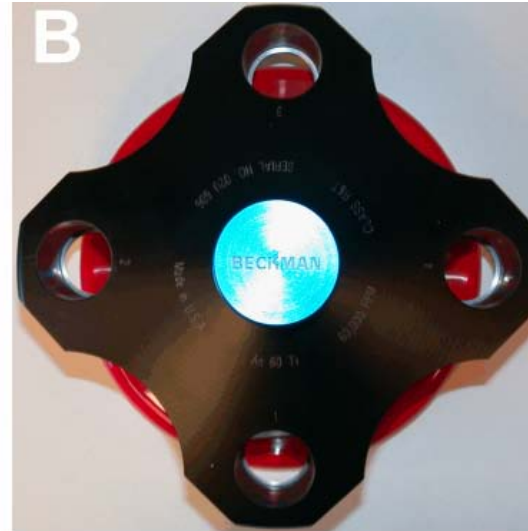


# Sample holders sit in holes in the AUC rotor

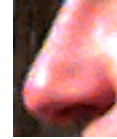
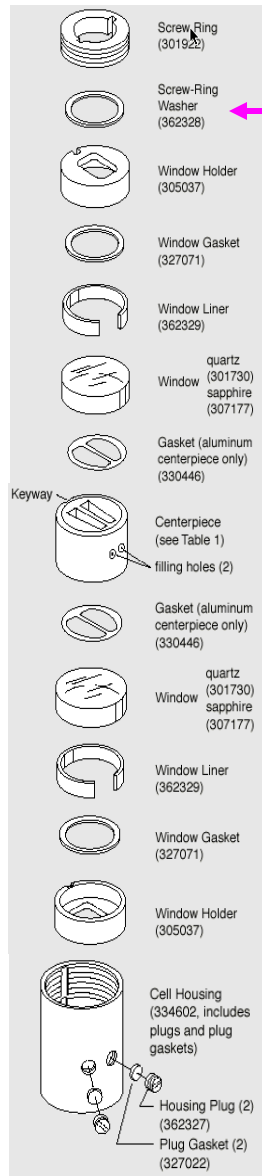
50k rpm



60k rpm



# The most difficult part of an AUC experiment: assembling the sample holders



Nose grease !!!

# Loading a sample

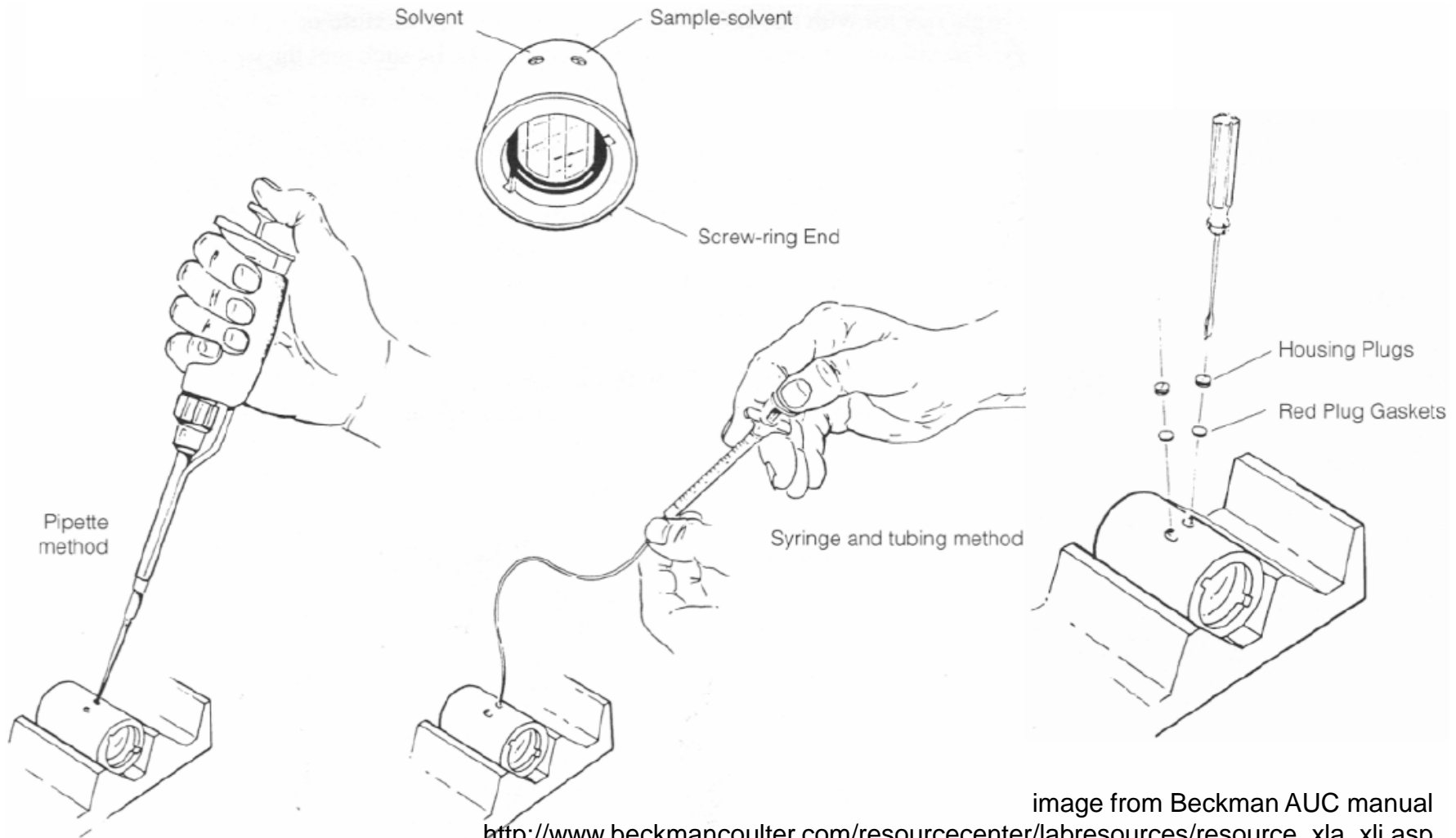


image from Beckman AUC manual

[http://www.beckmancoulter.com/resourcecenter/labresources/resource\\_xla\\_xli.asp](http://www.beckmancoulter.com/resourcecenter/labresources/resource_xla_xli.asp)

# Absorbance optics: the AUC is like a spinning double-beam spectrophotometer

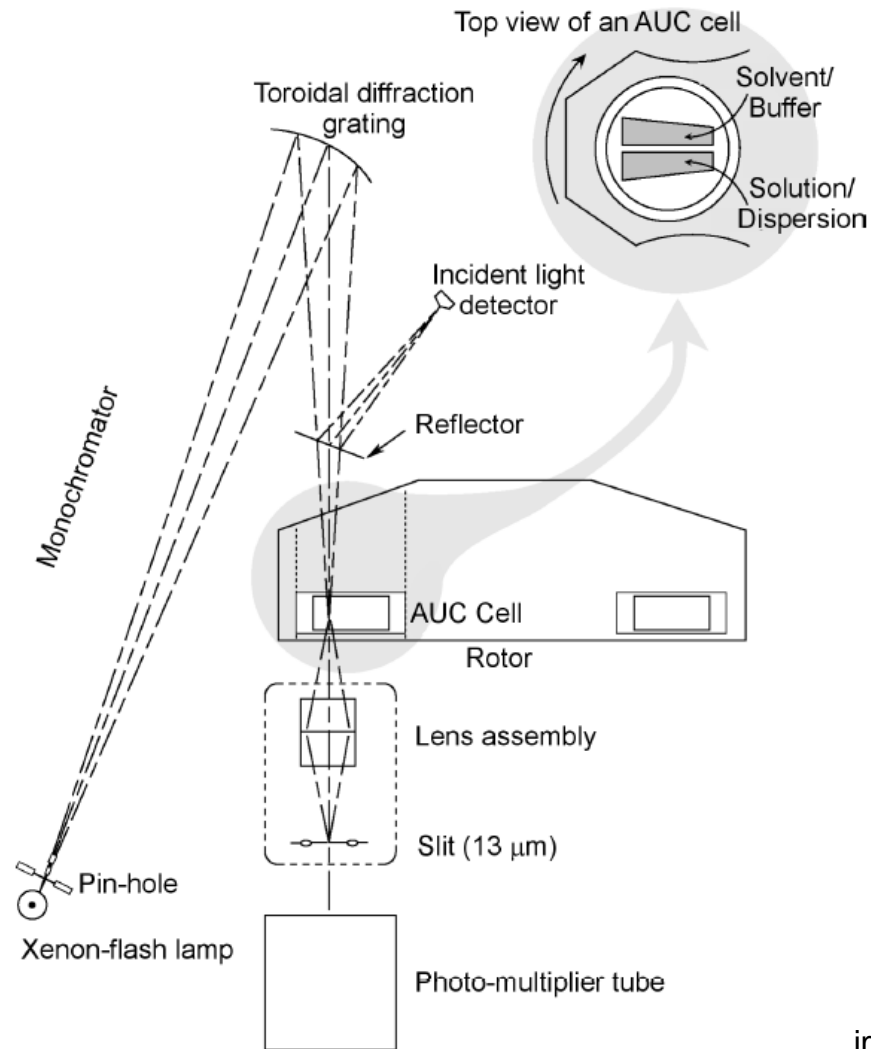


image from Beckman AUC manual

[http://www.beckmancoulter.com/resourcecenter/labresources/resource\\_xla\\_xli.asp](http://www.beckmancoulter.com/resourcecenter/labresources/resource_xla_xli.asp)

# Interference optics acquire refractive index data rapidly, independent of chromophores

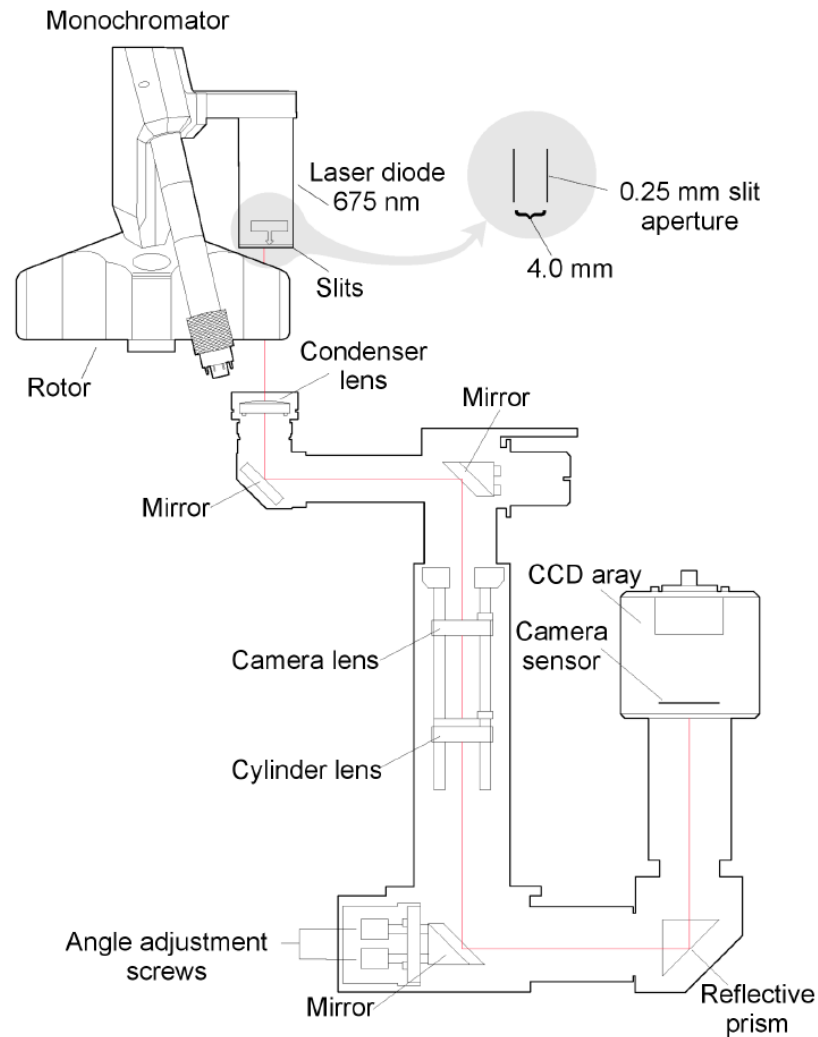


image from Beckman AUC manual

[http://www.beckmancoulter.com/resourcecenter/labresources/resource\\_xla\\_xli.asp](http://www.beckmancoulter.com/resourcecenter/labresources/resource_xla_xli.asp)

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## 2 modes of operation - several data types

- Sedimentation velocity (SV)
- Sedimentation equilibrium (SE)
  - In solution
  - Non-destructive
  - Self-cleaning
  - Absolute

# Comparison of all optical systems

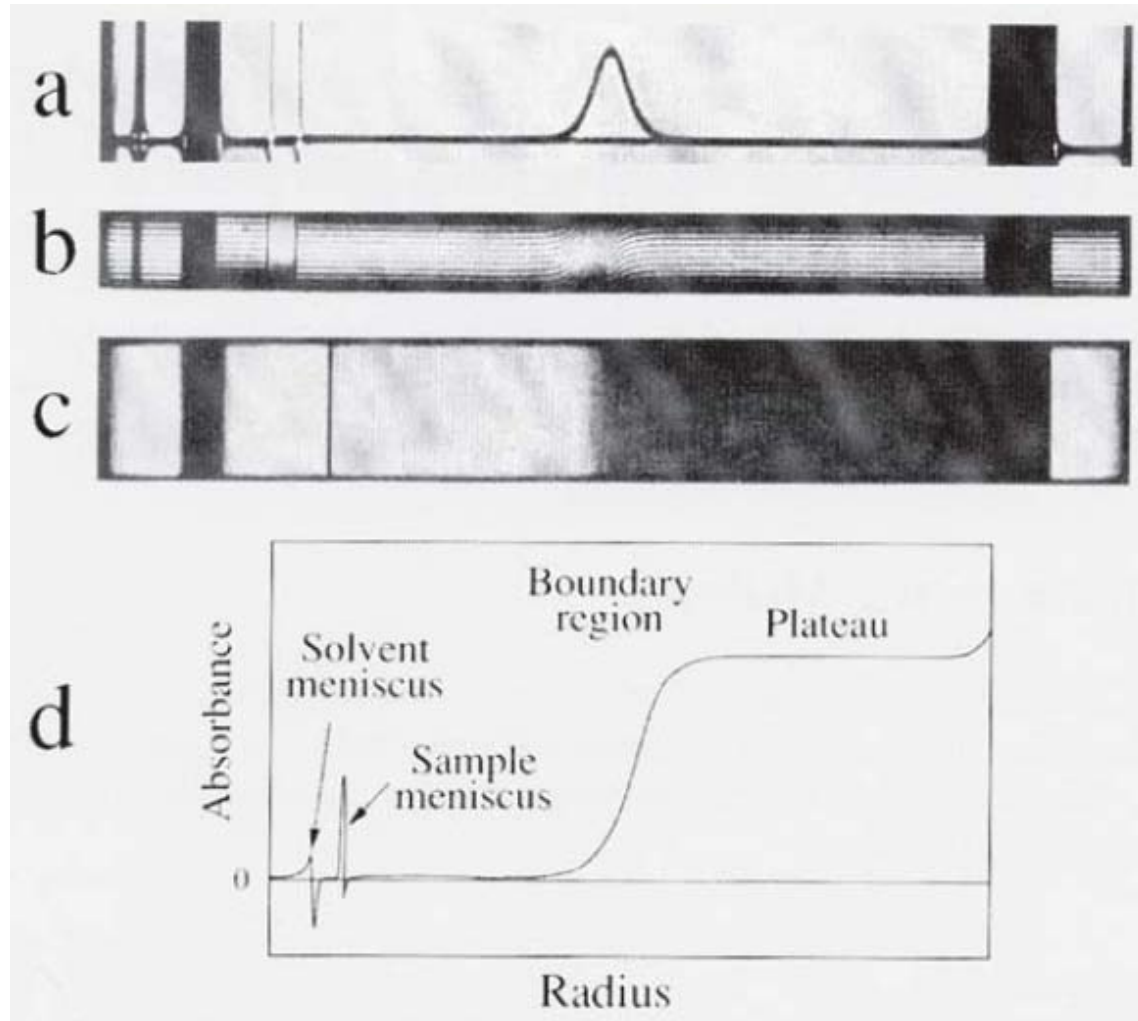


image from Ralston, 1993

<https://www.beckmancoulter.com/wsrportal/bibliography?docname=361847.pdf>

# Wanna buy an AUC?

- Choice of 2 instruments
  - Beckman Coulter ProteomeLab™ XL-A/XL-I (≈ €250k)
  - Spin Analytical CFA (available 3<sup>rd</sup> quarter 2014) (≈ \$200k)
    - <http://www.spinanalytical.com/cfa.php>



# CFA: Centrifugal Fluid Analyser – part of the Open AUC Project

Eur Biophys J (2010) 39:347–359

DOI 10.1007/s00249-009-0438-9

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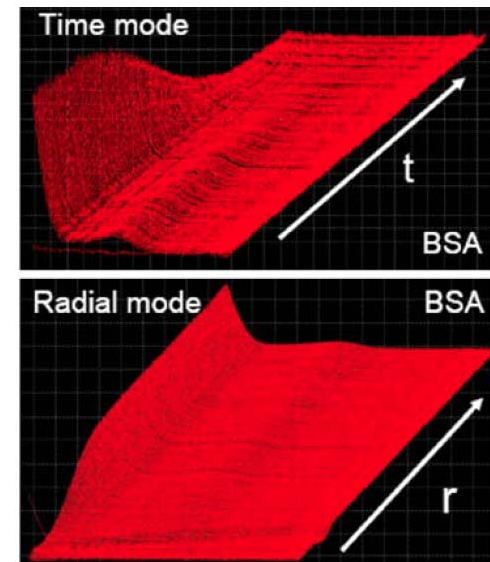
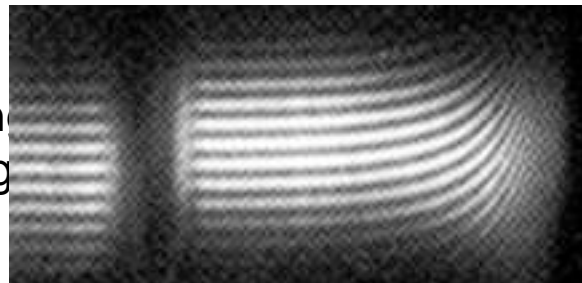
REVIEW

## **The Open AUC Project**

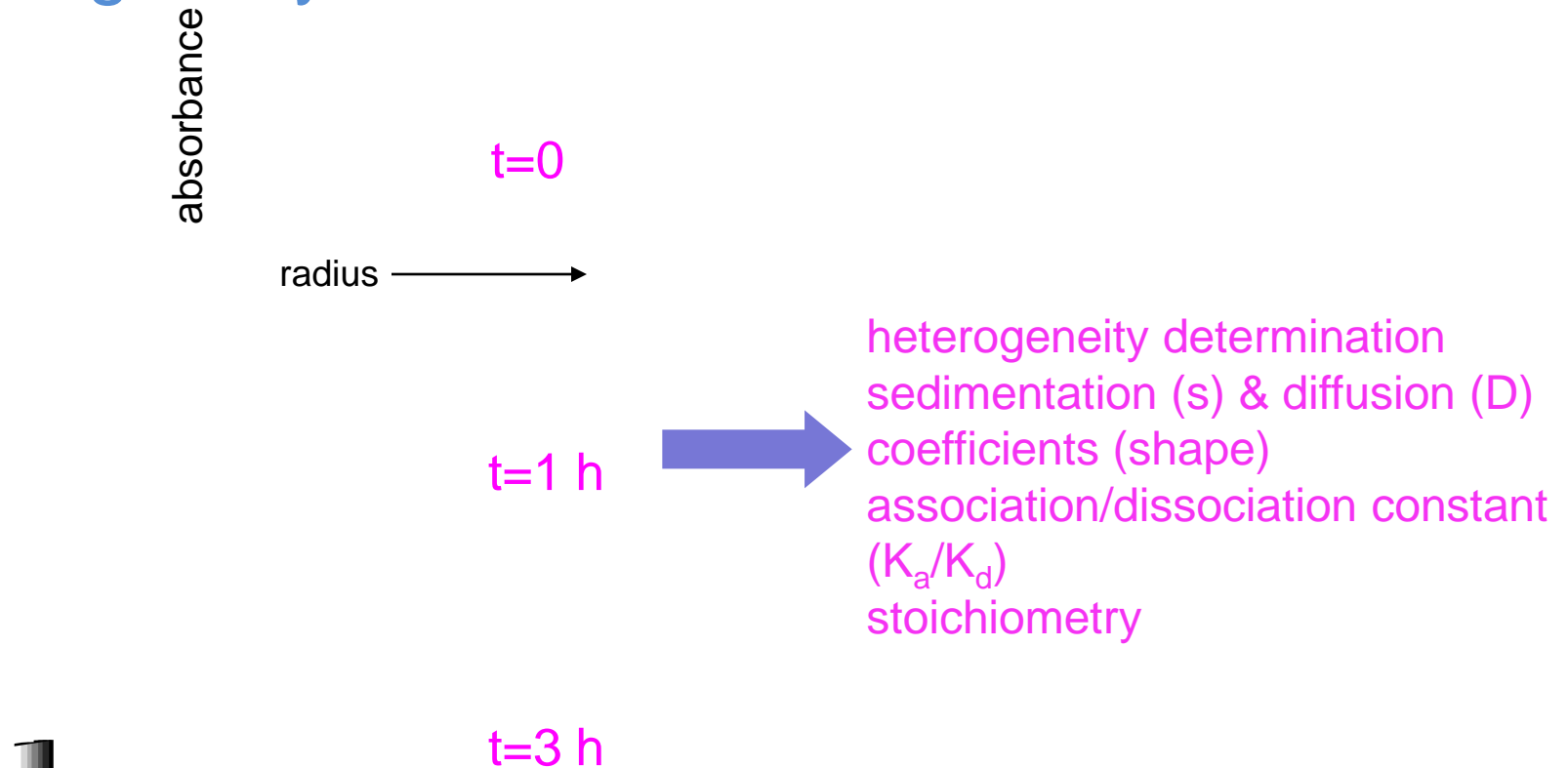
**Helmut Cölfen · Thomas M. Laue · Wendel Wohlleben · Kristian Schilling ·  
Engin Karabudak · Bradley W. Langhorst · Emre Brookes · Bruce Dubbs ·  
Dan Zollars · Mattia Rocco · Borries Demeler**

# The CFA is an entirely new AUC

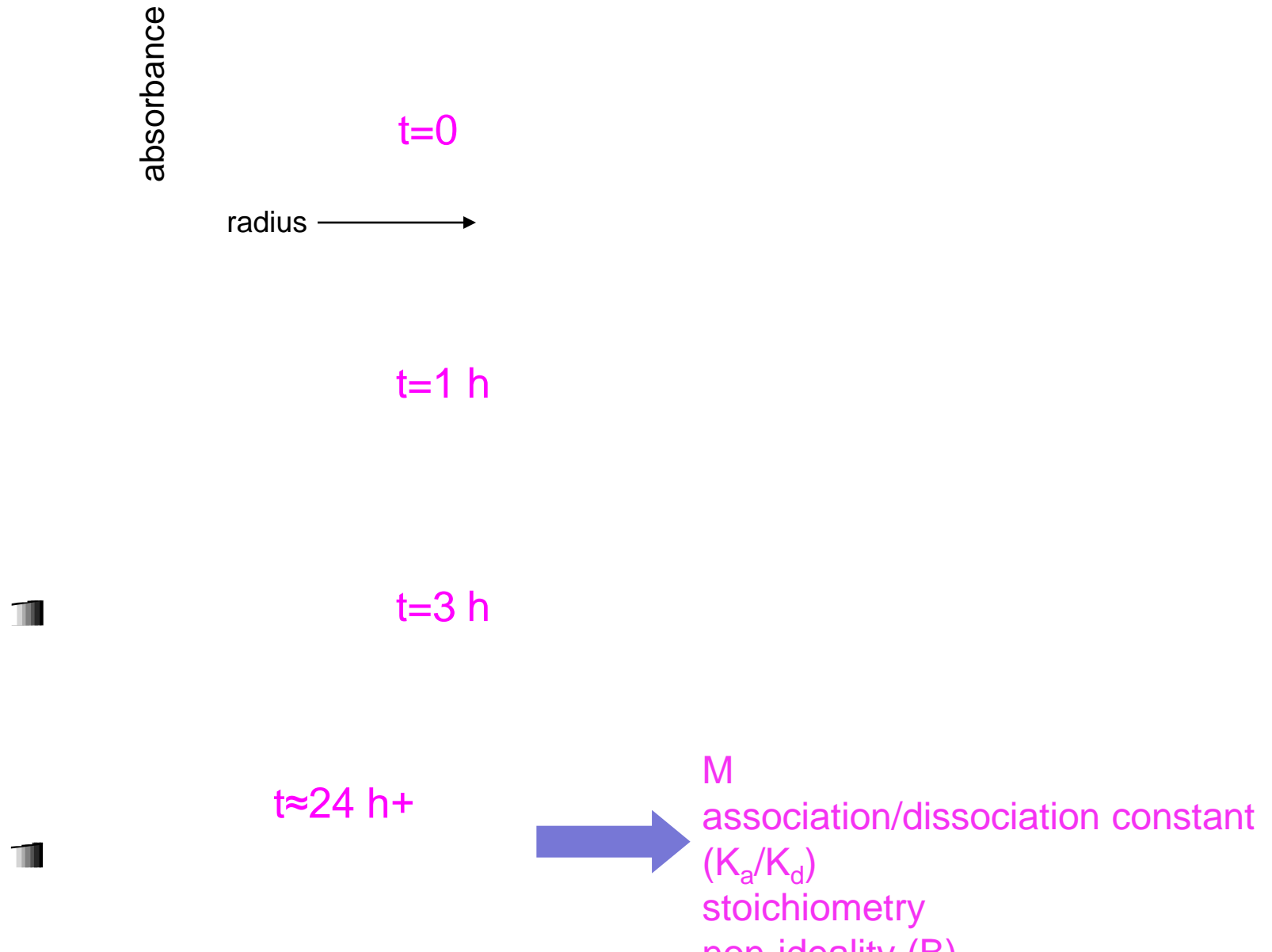
- Capacity for 3 optical systems
  - Detectors outside vacuum system
- Current
  - Dual Wavelength Fluorescence (DWF); permits:
    - 2 different fluorescently tagged molecules to be monitored simultaneously
    - FRET detection of molecular proximity of co-sedimenters
  - Multi-wavelength Absorbance (MWA); permits:
    - separation of components by absorbance spectrum & s
- Planned
  - Rayleigh interference
  - Schlieren refraction
  - Small-angle light scattering
  - Multi-angle light scattering (SAXS?)



# Sedimentation velocity (SV): shape & homogeneity



# Sedimentation equilibrium (SE): mass & self-association



# SV versus SE

- SV: observe movement of sedimentation boundary
- Change in (sometimes complex) boundary over time is due to
  - Sedimentation
  - Diffusion
- SE: rotor spun more slowly so diffusion can balance sedimentation - system reaches thermodynamic equilibrium
- Observe no change in boundary over time
  - Unless sample is degrading or changing in some other way



# Sample requirements

- **Sample volume**

- SV
  - 360  $\mu\text{l}$  (up to 480  $\mu\text{l}$ ) in 12 mm pathlength
  - 90  $\mu\text{l}$  (up to 120  $\mu\text{l}$ ) in 3 mm pathlength
- SE
  - 20  $\mu\text{l}$  (8-channel centrepiece - interference optics only)
  - 80  $\mu\text{l}$  (2- or 6-channel centrepiece)

- **Sample concentration**

- Absorbance optics:  $A_{\lambda} \approx 0.1-1.0$  in 12 mm pathlength cell
  - $\lambda = 180-800$  nm
- Interference optics: typically 0.05-30 mg/ml

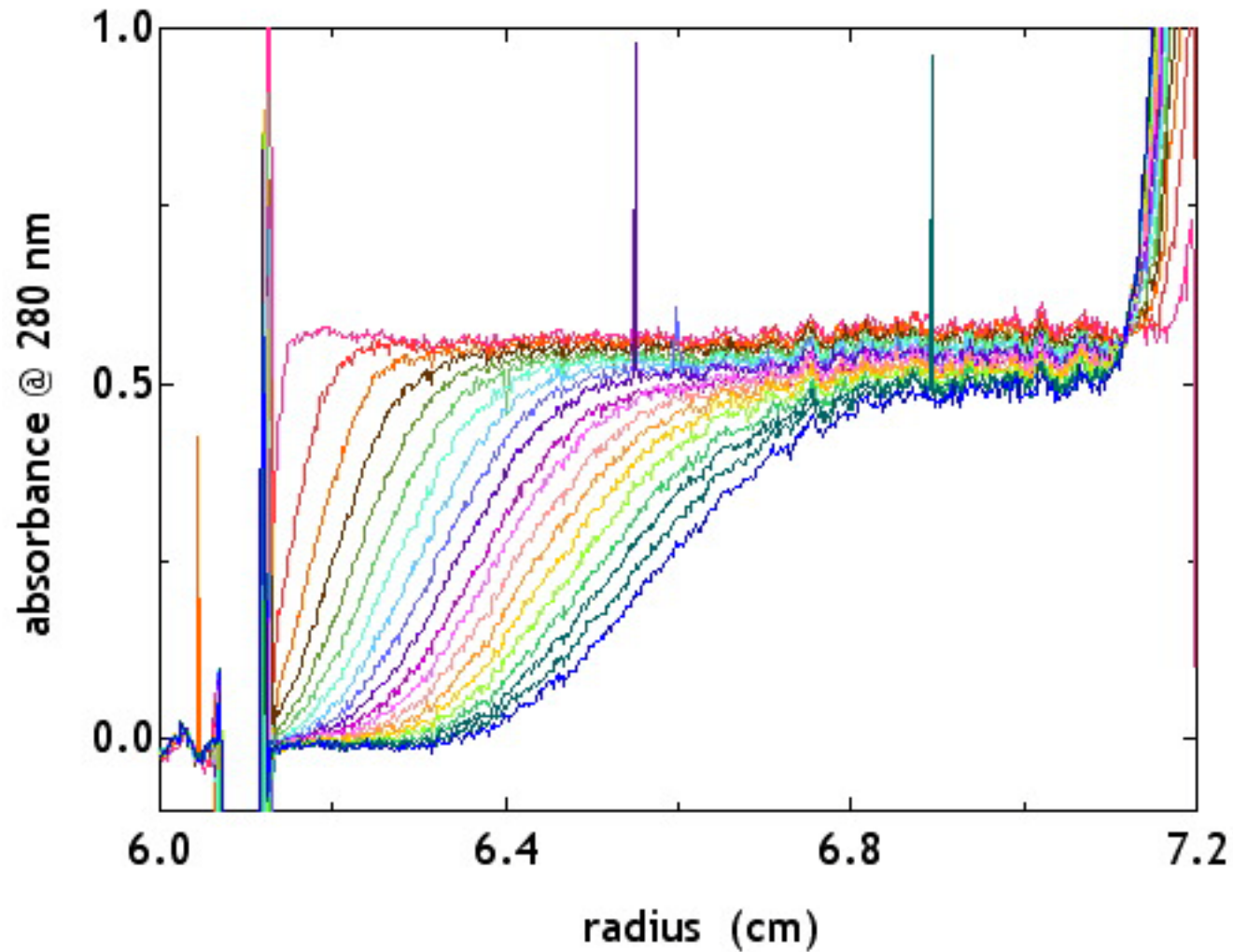
- **Sample reference**

- Absorbance optics: can be column eluant or dialysate better
- Interference optics: must be dialysate

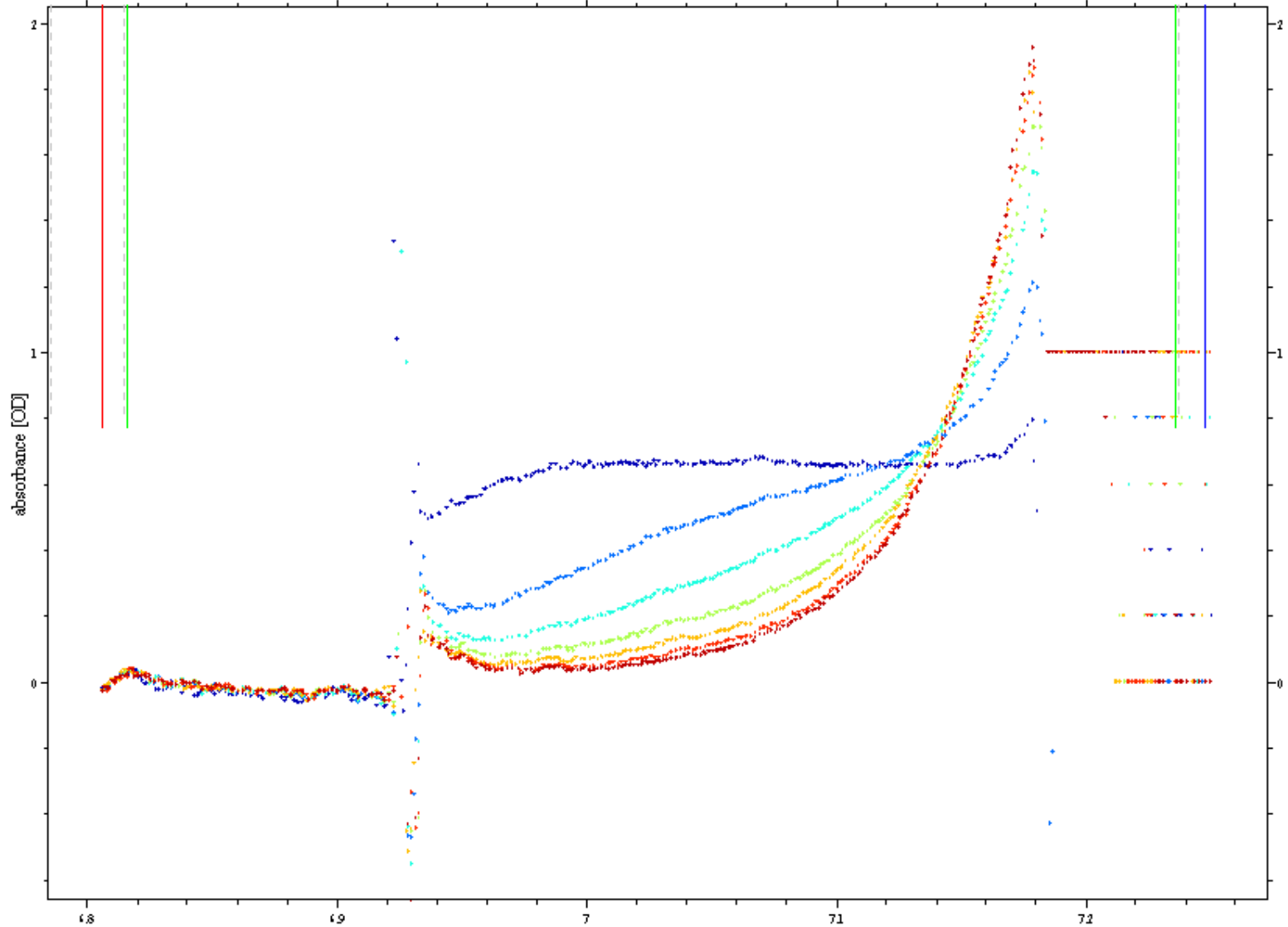
- **Typical multiplexing: 3 or 7 sample holders (“cells”)/run**

- Up to 28 samples per run

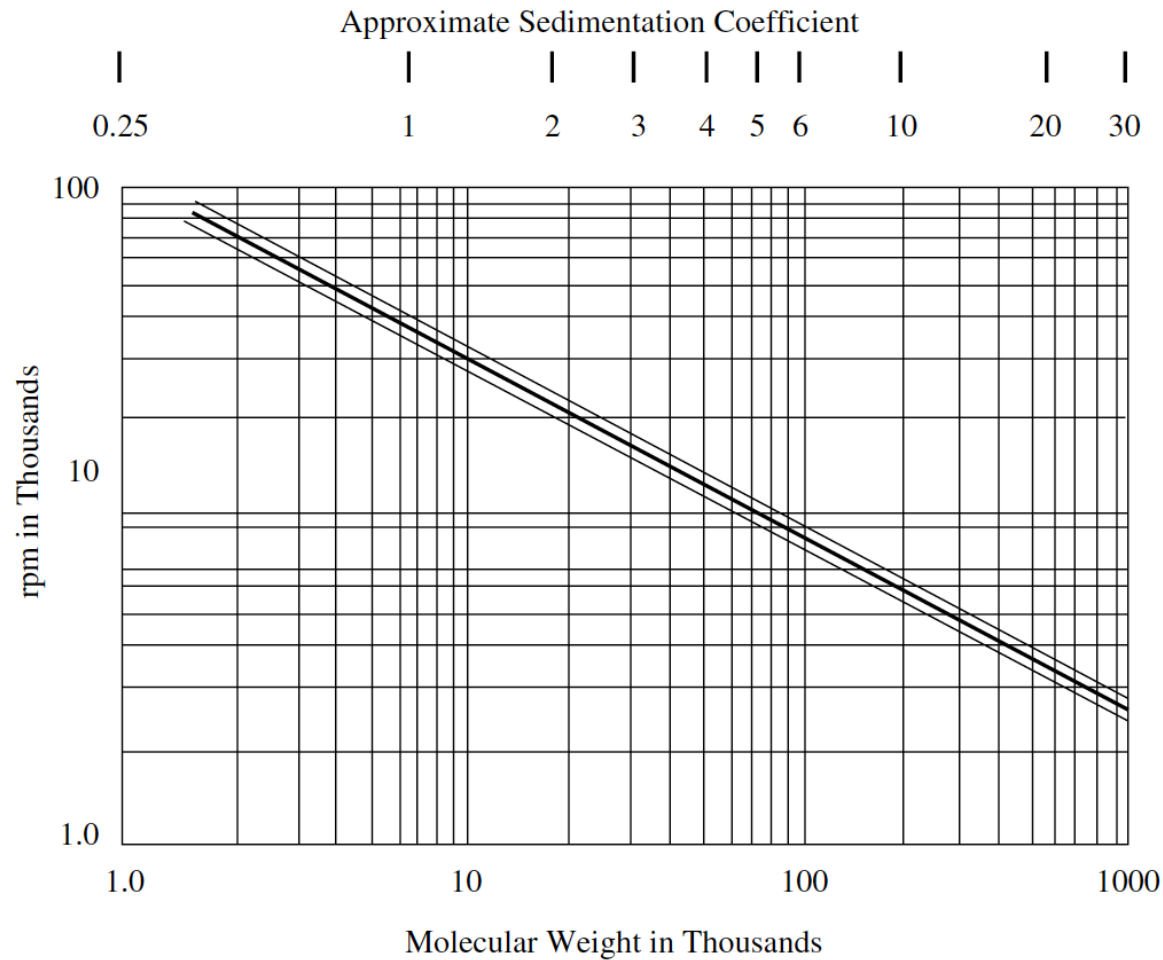
# SV: radial movement recorded as function of time



# SE: data recorded until no change



# Which speed?



Chervenka, C. H. *A Manual of Methods for the Analytical Ultracentrifuge*.  
Spinco Division, Beckman Instruments, Palo Alto, 1969

# Which speed?

- Rotor speed chosen to optimise shape of equilibrium distribution
- Rule of thumb: at lowest chosen rotor speed, effective molecular weight ( $\sigma$ ) = 1

$$\sigma = \frac{M(1 - \bar{v}\rho)\omega^2}{RT}$$

- At subsequent speeds, speed factor = 1.5

$$\text{Speed Factor} = \frac{\omega^2 \text{ for Speed 2}}{\omega^2 \text{ for Speed 1}}$$

- Ensures that in global fitting of data at different speeds, data are different from each other

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## 3 important equations

$$s = \frac{u}{\omega^2 r} = \frac{M(1 - \bar{v}\rho)}{N_A f}$$

Svedberg equation

$$D = \frac{sRT}{M(1 - \bar{v}\rho)}$$

Lamm equation

$$\frac{dc}{dt} = \frac{l}{r} \frac{d}{dr} \left[ rD \frac{dc}{dr} - s\omega^2 r^2 c \right]$$

# Almost all AUC data analysis software is freely available

- **The RASMB website**
  - “Reversible Associations in Structural and Molecular Biology”
  - <http://www.rasmb.bbri.org/>
  - Access to freely available software
  - Subscription to AUC-related discussion group
- **Schuck lab (SEDFIT, SEDPHAT)**
  - <http://www.analyticalultracentrifugation.com/default.htm>
- **Demeler lab (UltraScan III (including SOMO))**
  - <http://www.ultrascan.uthscsa.edu/>



# Many methods & programs for SV data analysis

- Too many for comprehensive review here
- Model independent:
  - $dc/dt$  (Stafford, SedAnal)
    - Eliminates time invariant noise. Resultant curves can be fitted with Gaussians to reveal species content and sedimentation coefficients.
  - $c(s)$  (Schuck, Sedfit)
    - Good for “first look” at data to get an idea of number of species. Not a proper fit to data.
  - van Holde-Weischet (Demeler, UltraScan III)
    - Diffusion corrected  $s$  distribution. Good for detection of aggregates and identification of underlying model.
- Model dependent:
  - Non-interacting discrete species (Schuck, Sedfit)
    - Up to 4 separate species can be fitted.
  - Self-association (Stafford, SedAnal; Demeler, UltraScan III)
    - Determination of  $K_d$ ,  $k_{on}$ ,  $k_{off}$ , stoichiometry

$s$  is influenced by solvent density & viscosity and sample density

sample partial  
specific volume

solvent density

solvent  
viscosity

$s_{20,w}$

$$= \frac{(1 - \bar{v}\rho)_{20,w}}{(1 - \bar{v}\rho)_{T,b}} \frac{\eta_{T,b}}{\eta_{20,w}} s_{T,b}$$

sedimentation coefficient  
standardised to solvent  
of water @ 20°C

≈ 1.5 for typical  
aqueous solvent at  
4°C

experimental sedimentation  
coefficient determined in  
e.g. buffer (b) at T°C

# SEDNTERP : Calculation of $\rho$ , $\eta$ and partial specific volume online

The screenshot shows the SEDNTERP web application interface. The browser address bar displays "sednterp.unh.edu". The application has a menu bar with "File" and "Help". Below the menu bar are tabs for "Sample", "Solvent", "Experiment", and "Results".

**Buffer Data**  
Select from list to retrieve from database  
New Solvent

**Density**  
Direct Entry Standard Compute

**Viscosity**  
Direct Entry Standard Compute

**pH**

**Calculate Buffer Density**  
Density 1.00790 Density Corrected for Temperature & Isotopes of Water 1.00790

**Calculate Buffer Viscosity**  
Viscosity 0.01002 Viscosity Corrected for Temperature 0.01002

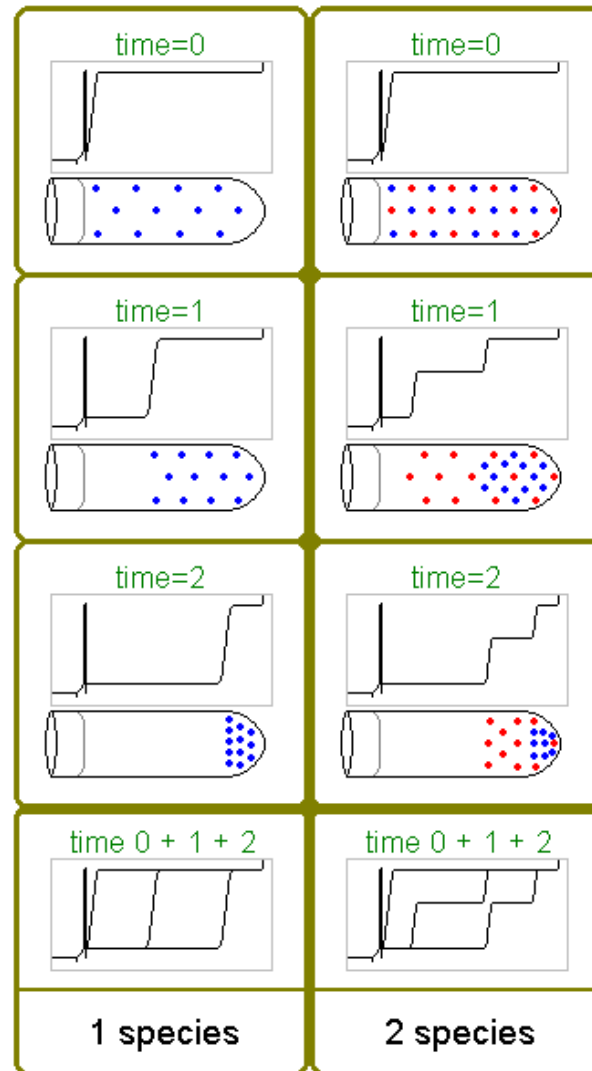
**Components**  
--Select-- Add =>

Buffer Components	Concentration	Concentration Units
Sodium chloride	0.2	molar
Tris(hydroxymethyl)aminomethane	0.05	molar

**Heavy Isotopes of water**  
H<sub>2</sub>O 100 % Volume  
D<sub>2</sub>O 0 % Volume  
H<sub>2</sub>O<sub>18</sub> 0 % Volume  
D<sub>2</sub>O<sub>18</sub> 0 % Volume

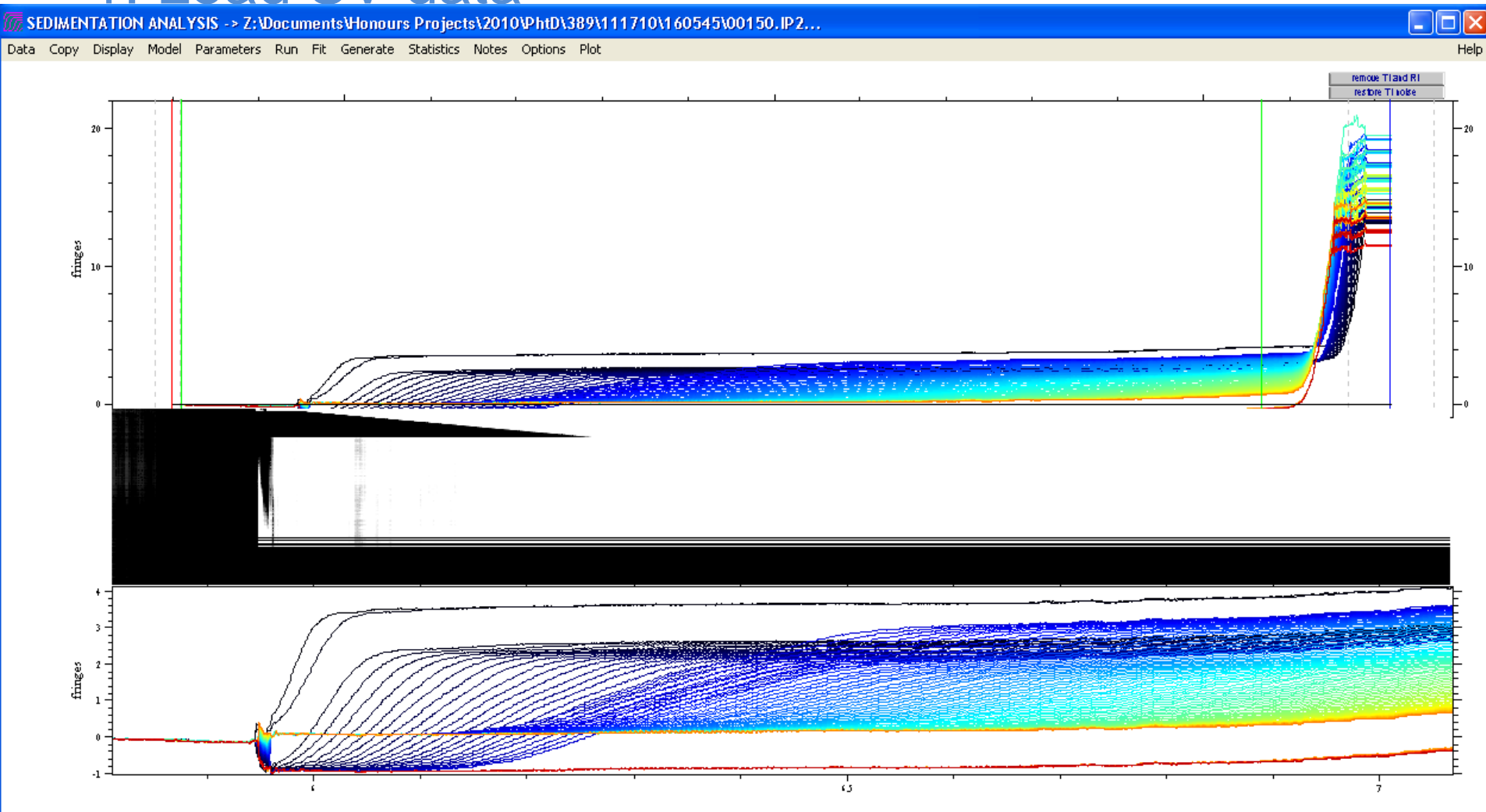
Cancel Ok

# SV: species can resolve into separate boundaries

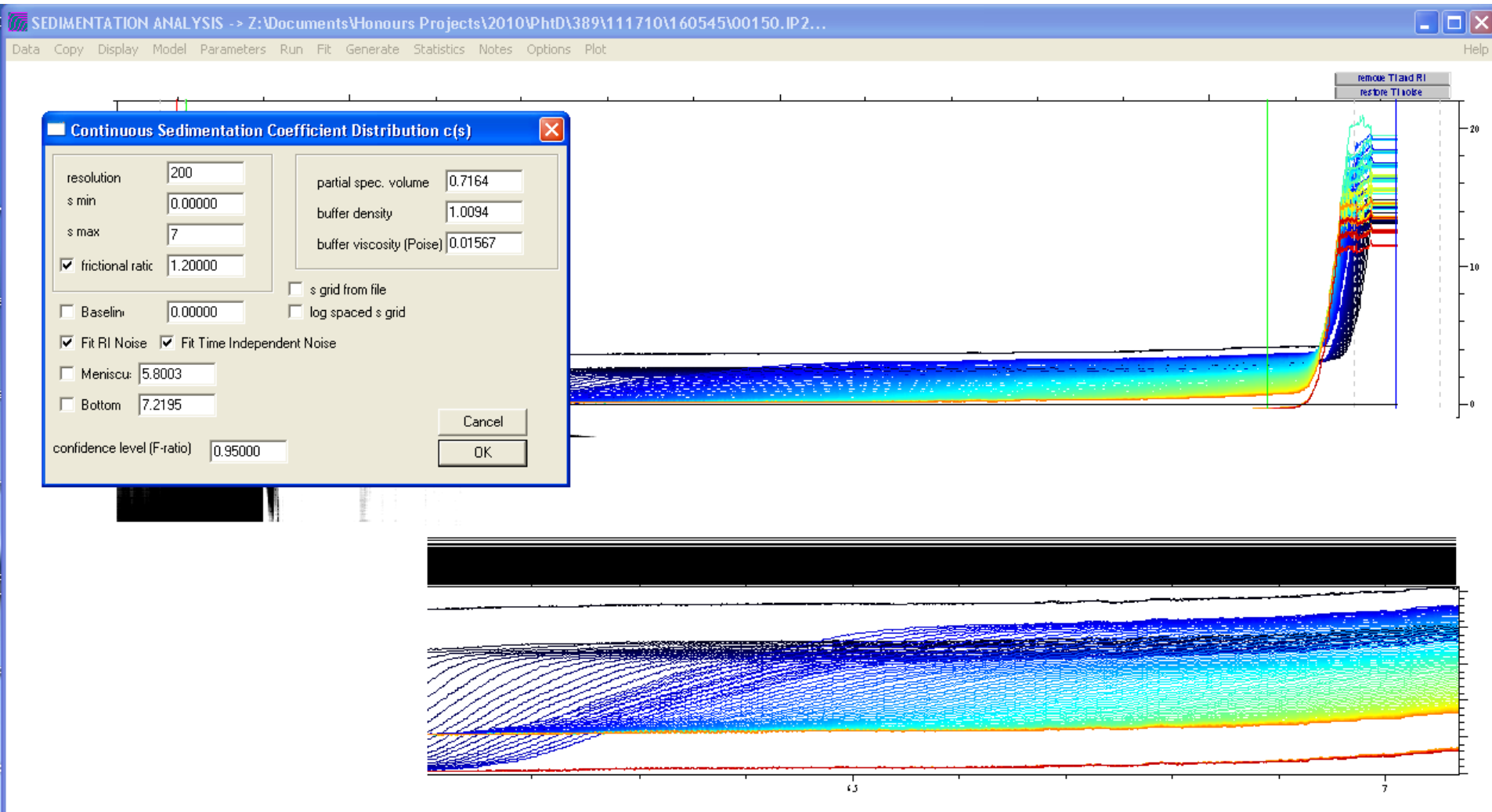


# SEDFIT c(s) analysis: how many species + s of species

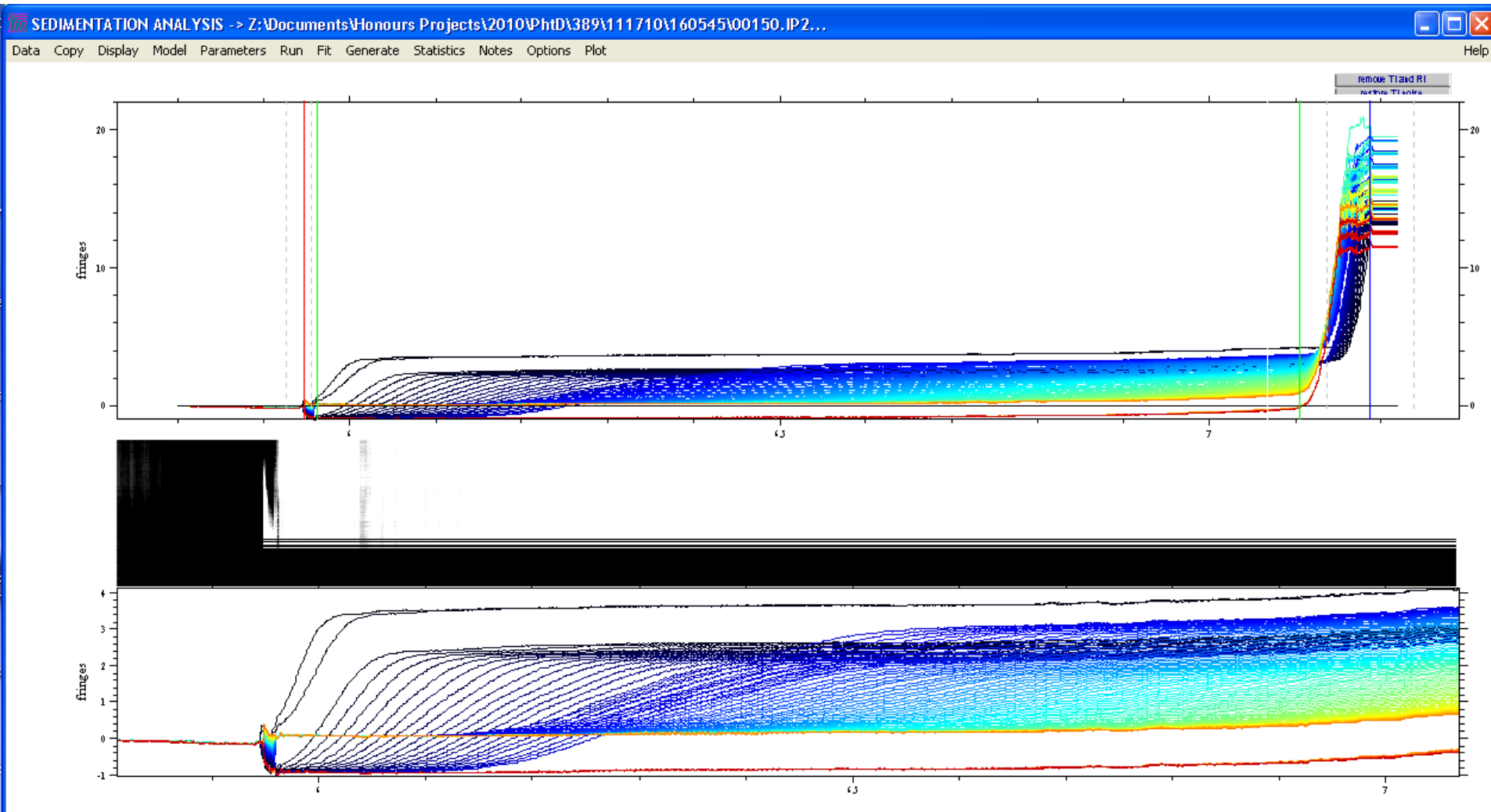
## 1: Load SV data



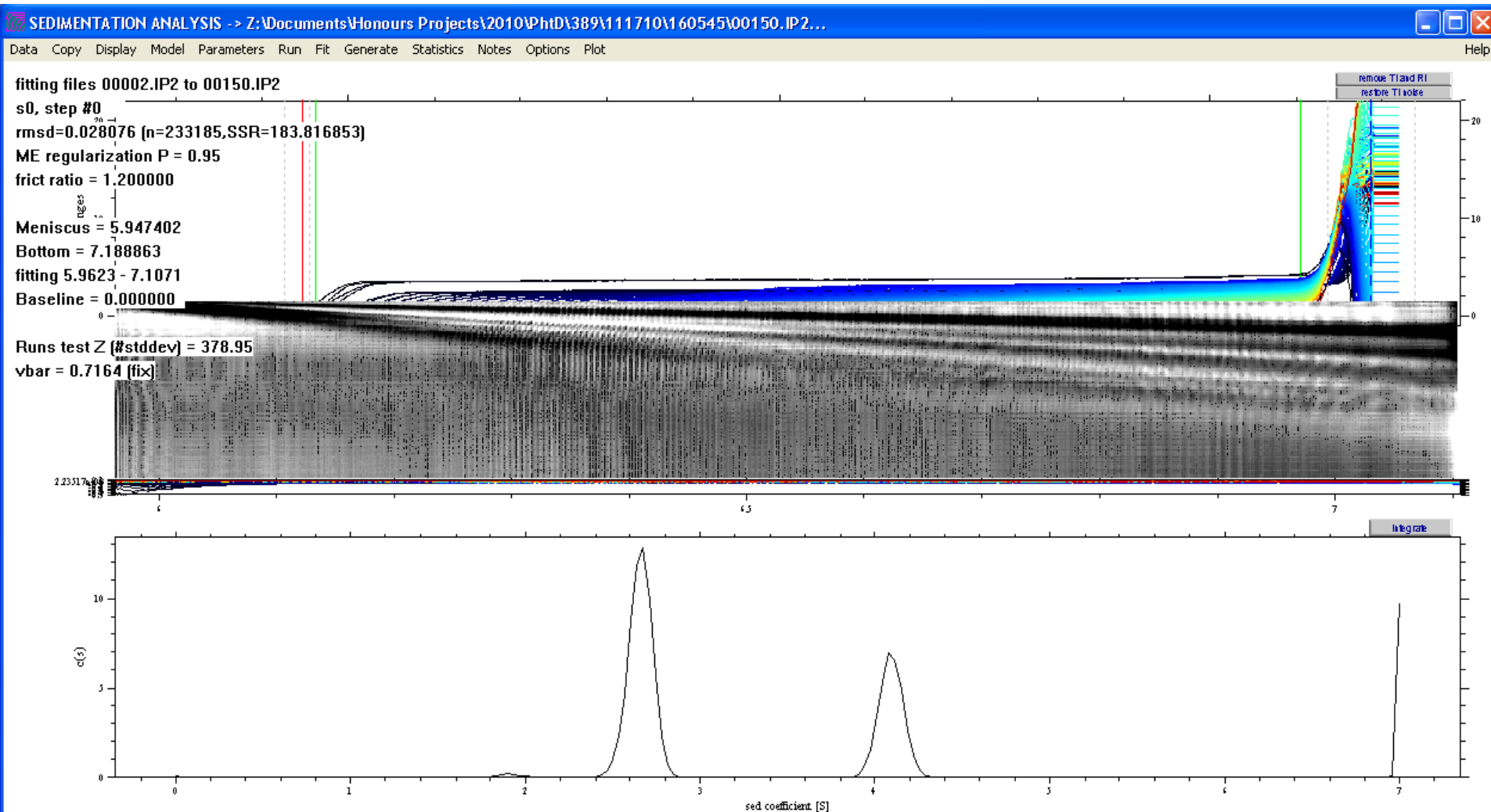
# 2: Specify parameters



# 3: Set meniscus, cell base and analysis limits

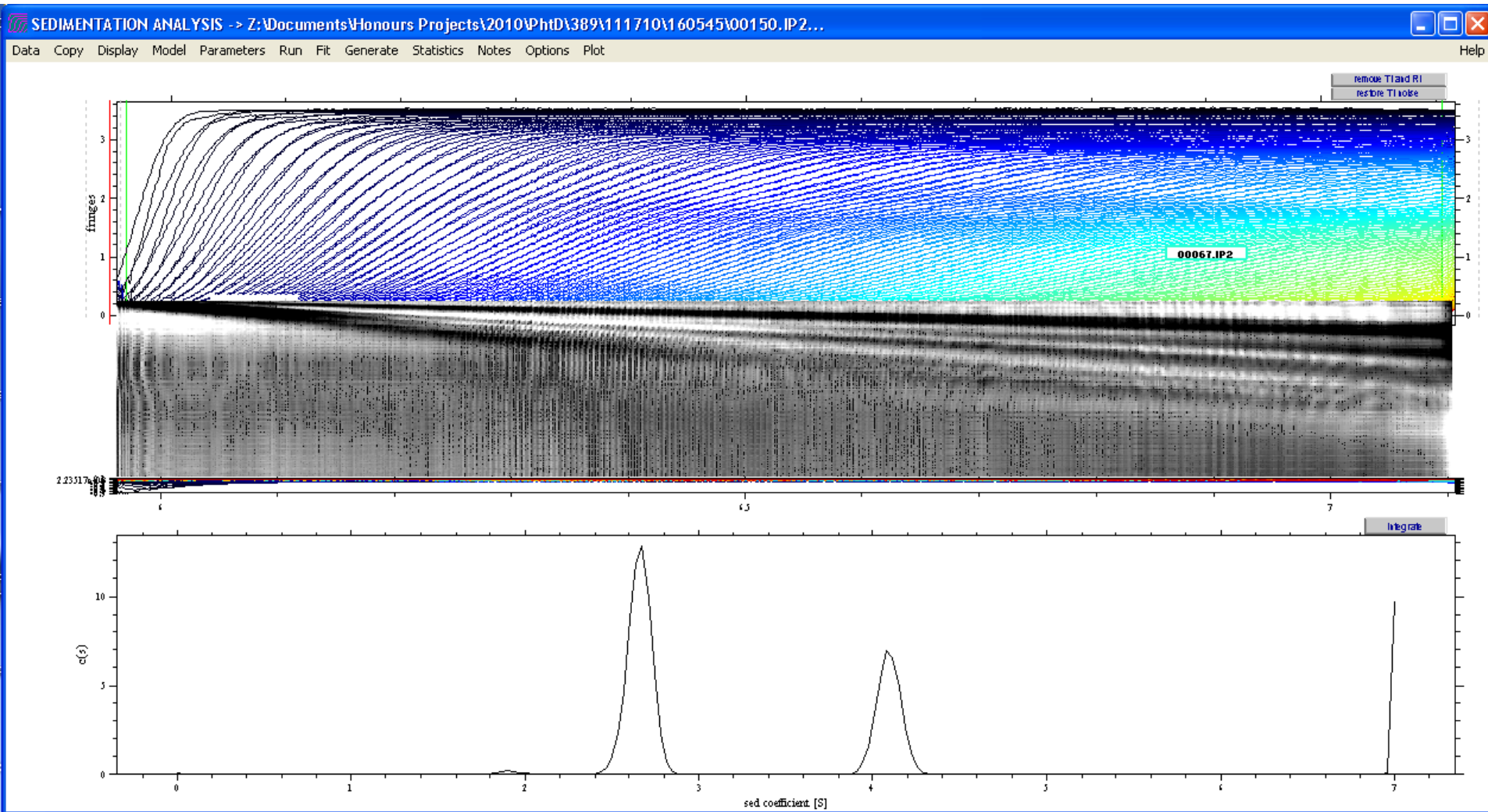


# 4: Run

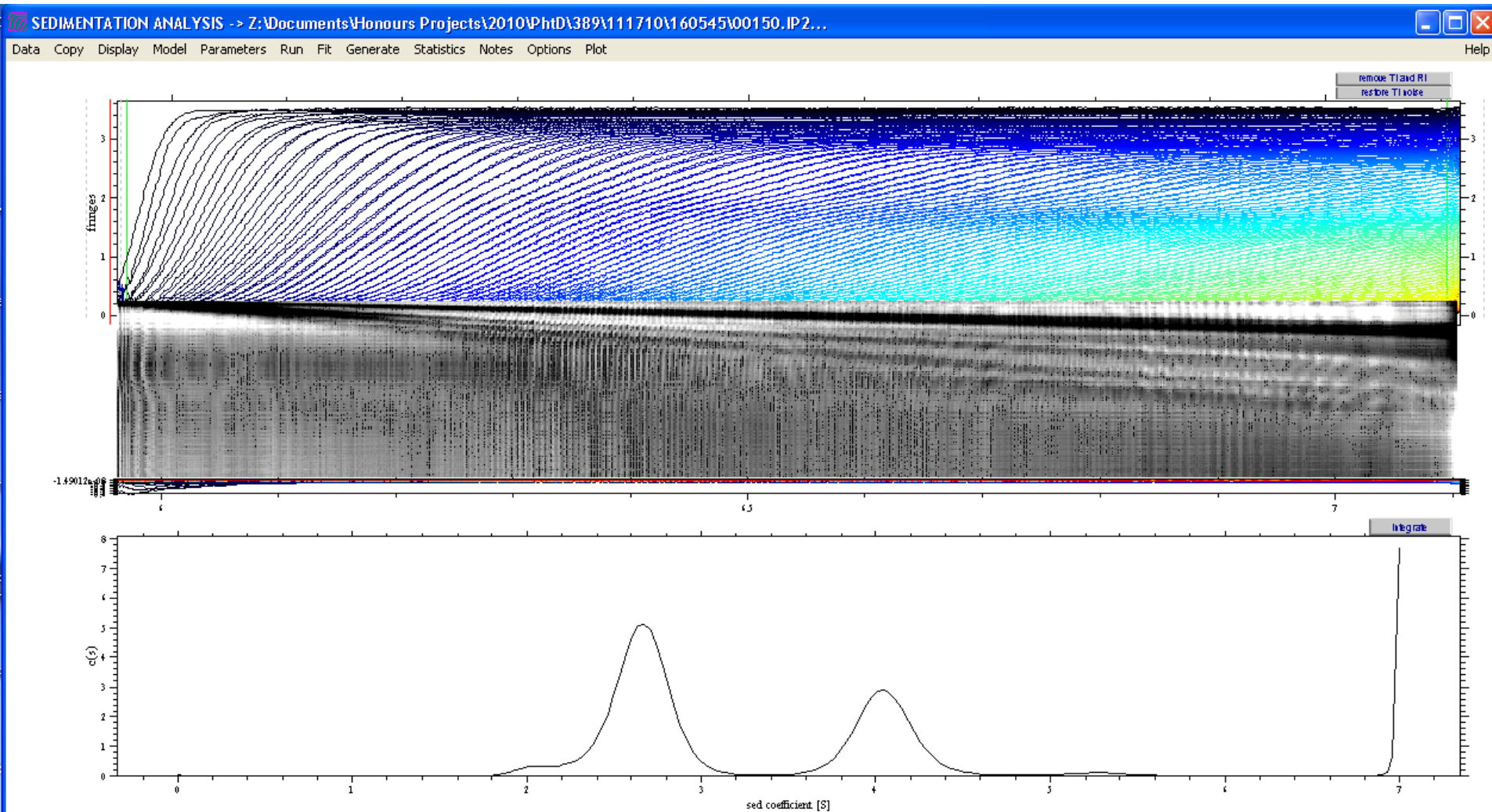




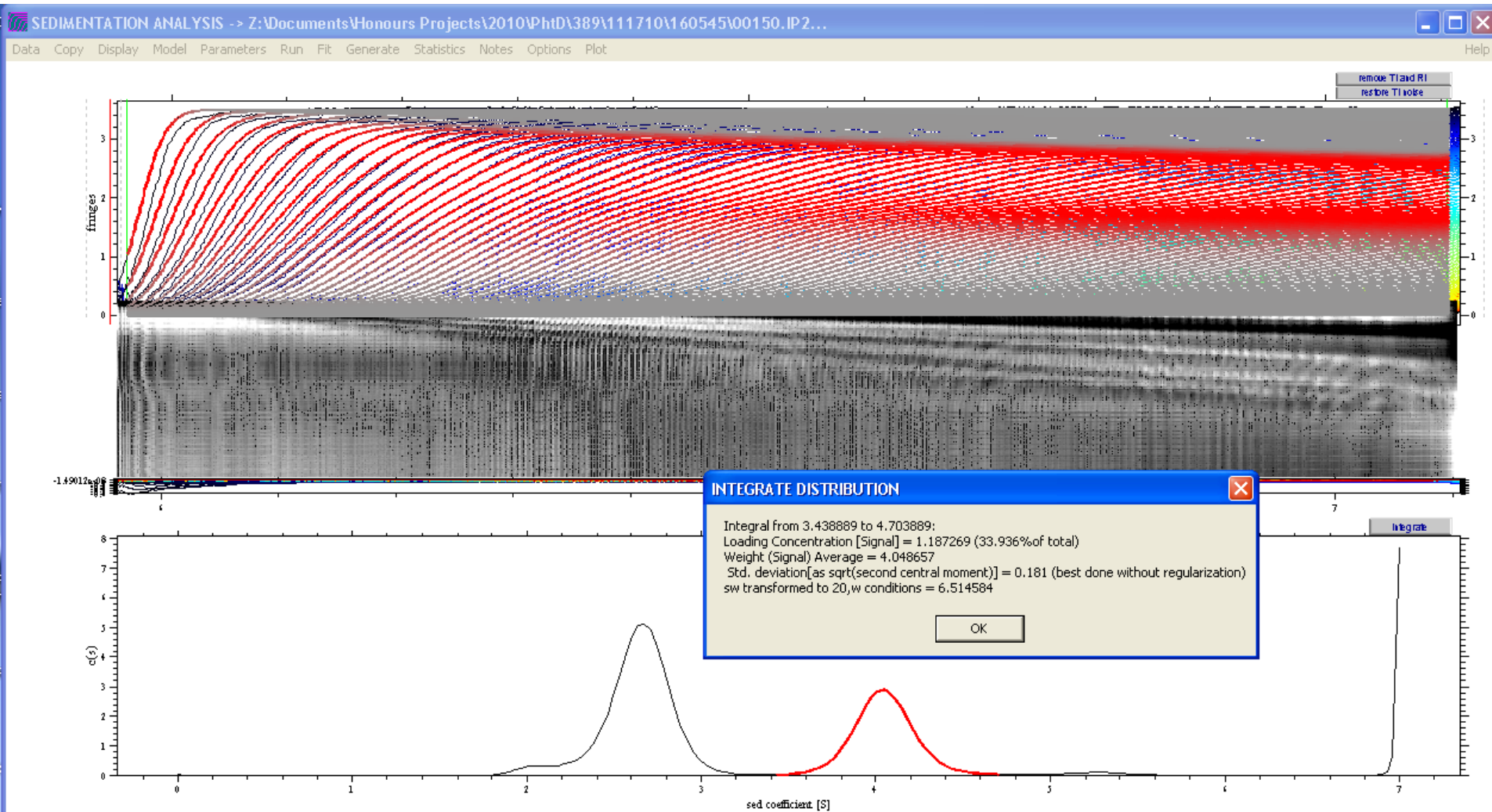
# 5: Subtract time and radial invariant noise



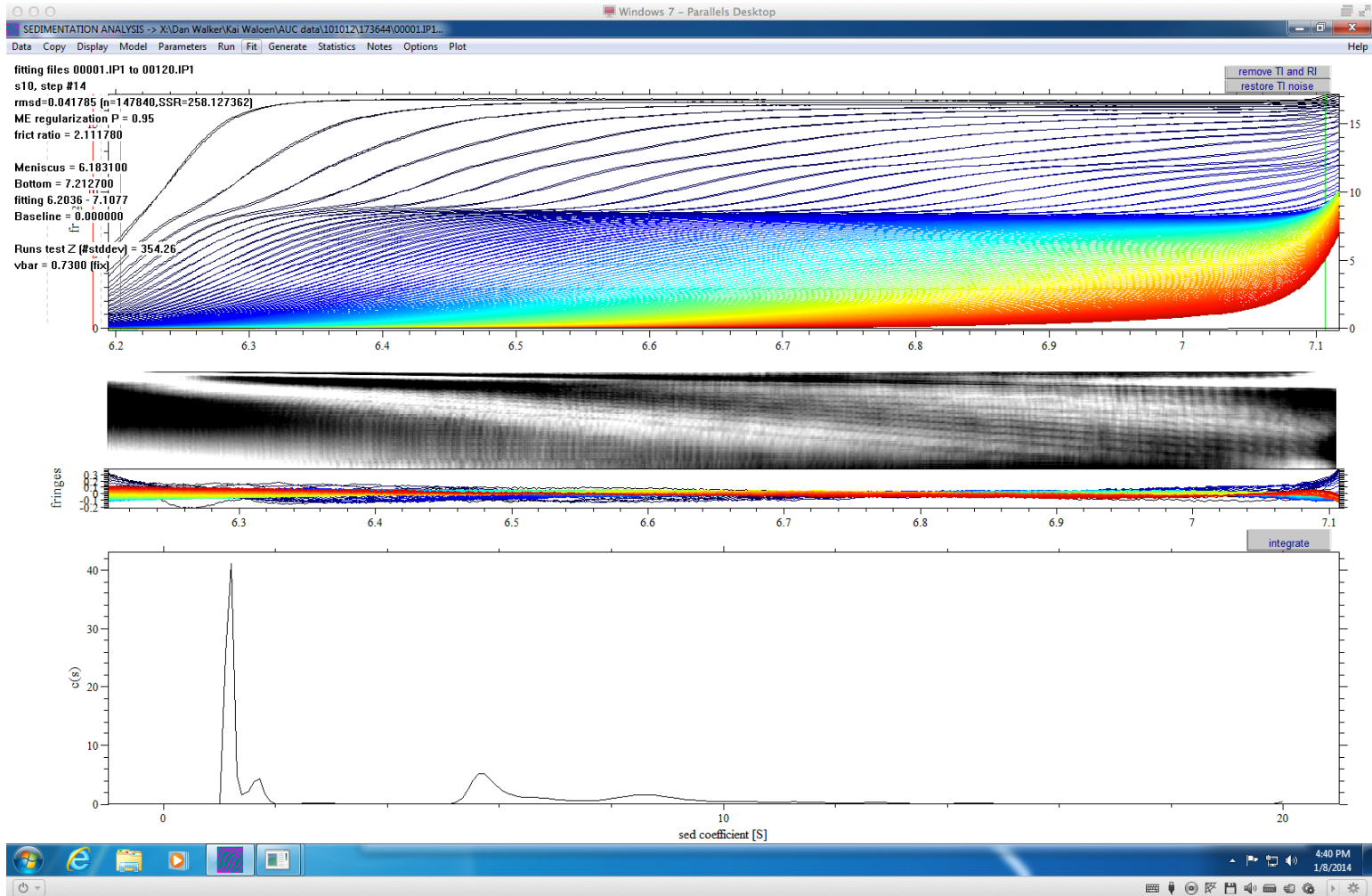
# 6: Fit (with solutions to the Lamm equation)



# 7: Integrate to obtain estimate of concentration of species and weight-average values

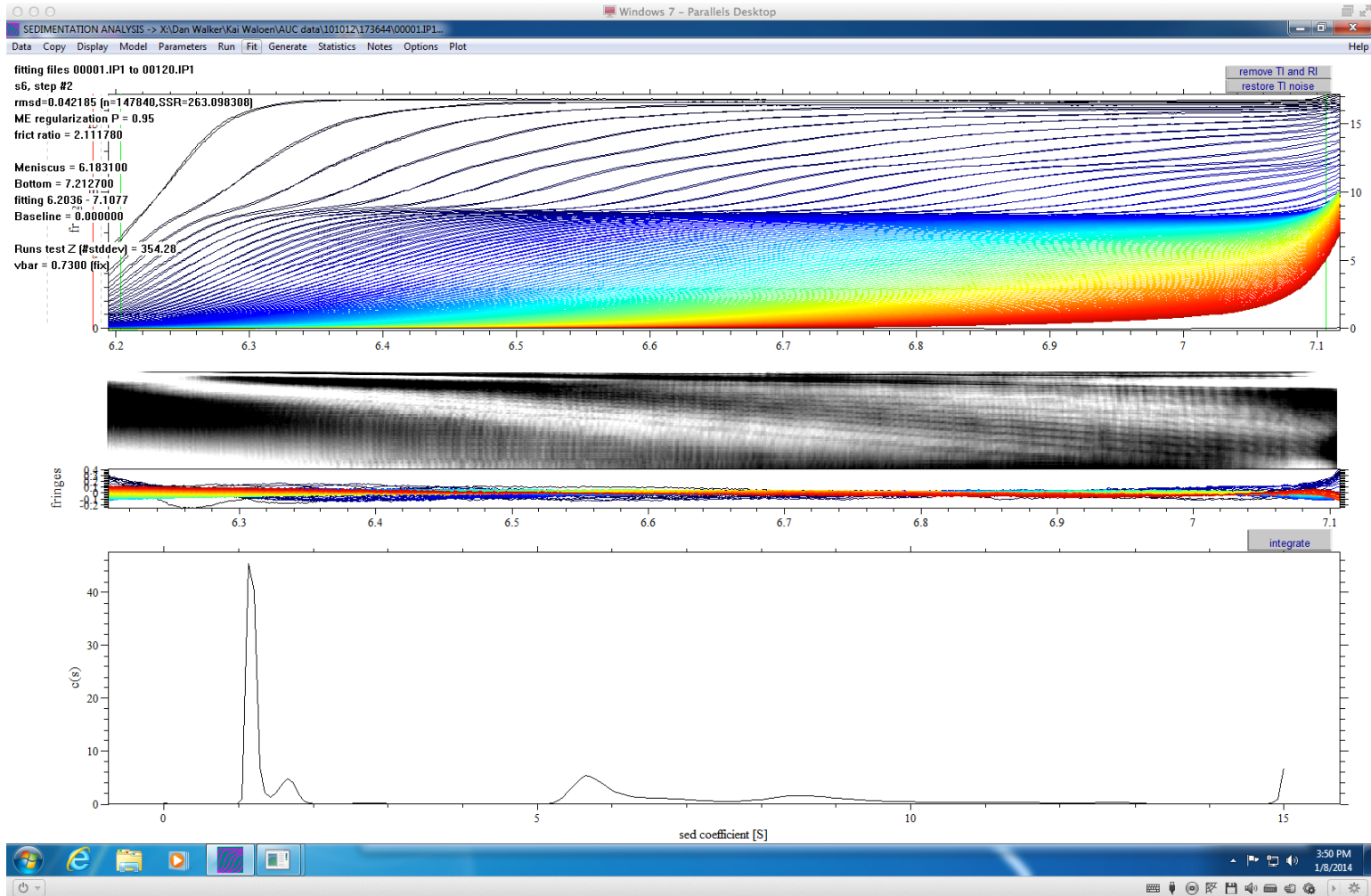


# Sum of Lamm equations $0 \leq s \leq 20$ S discretised by 200

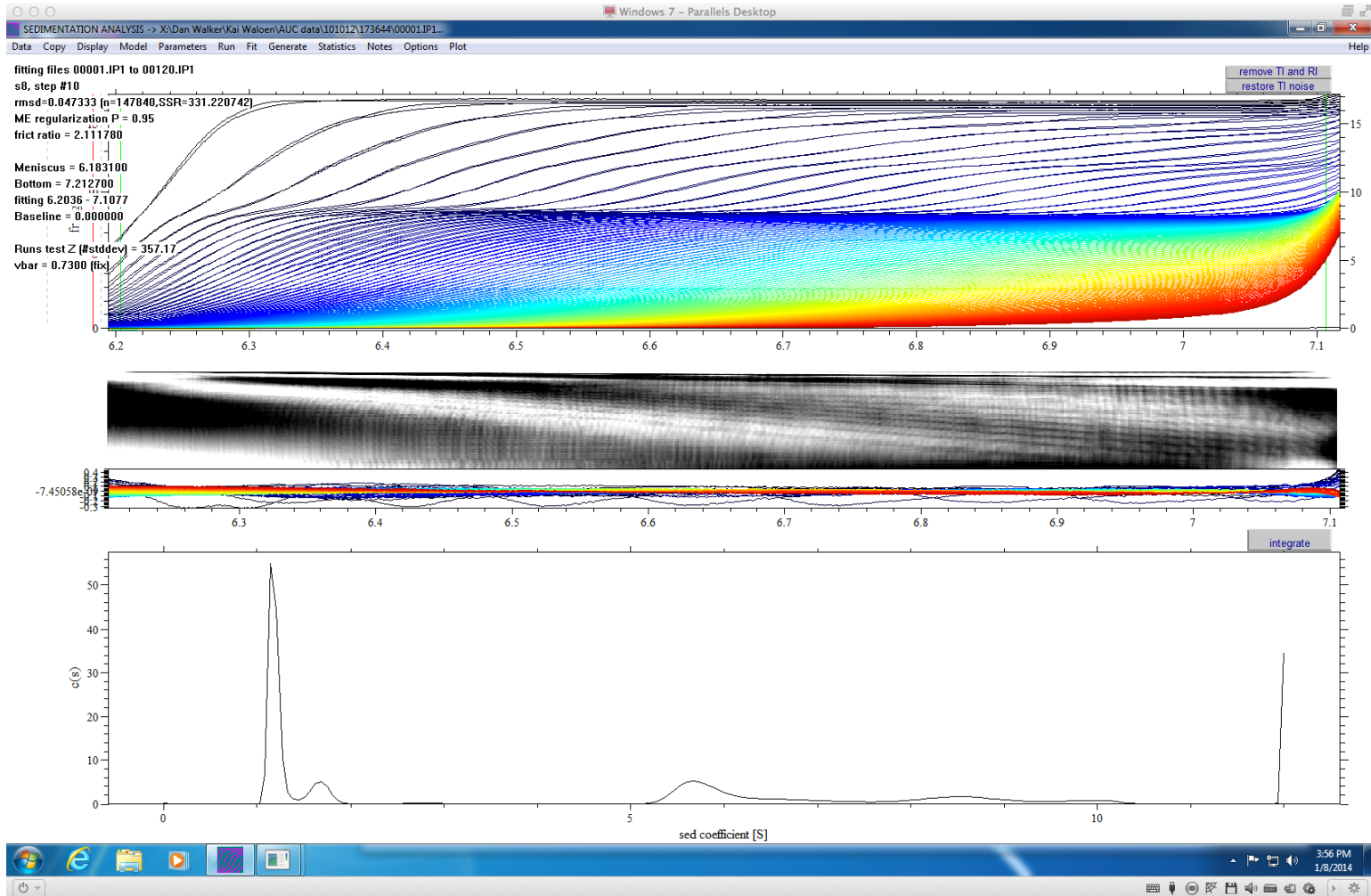




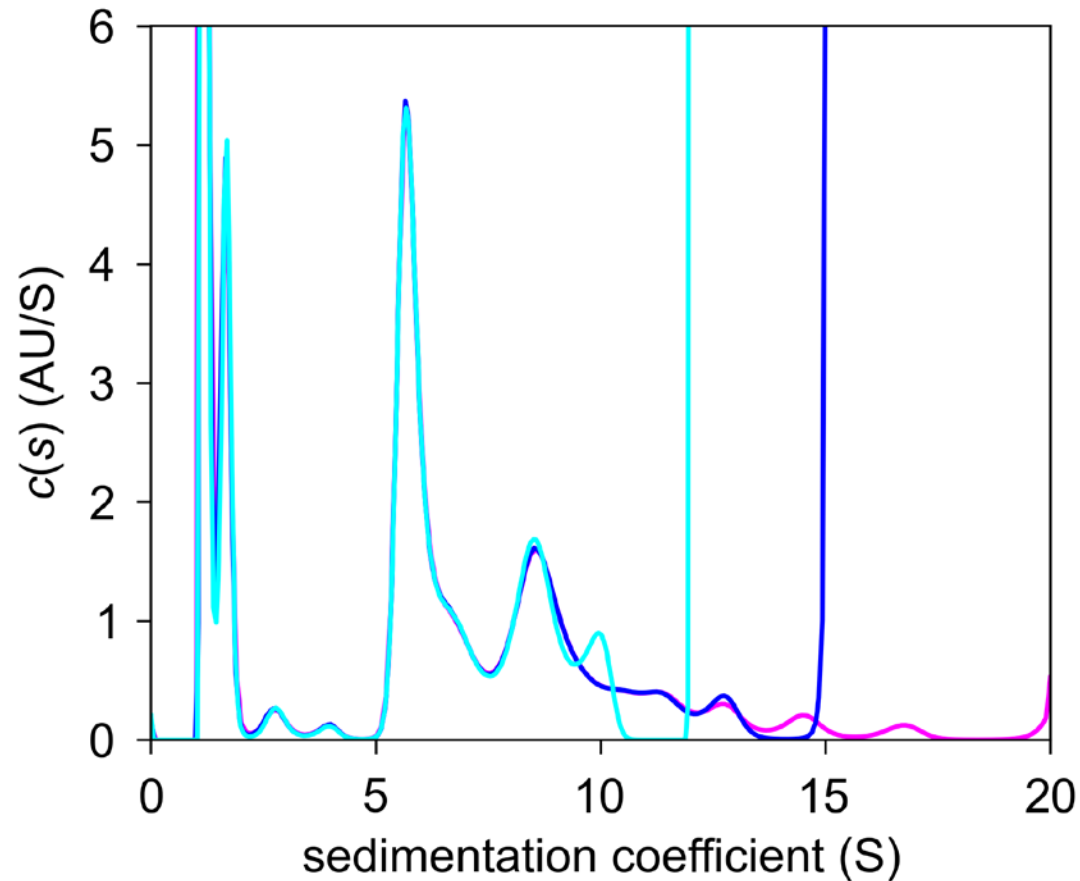
# Sum of Lamm equations $0 \leq s \leq 15$ S discretised by 200



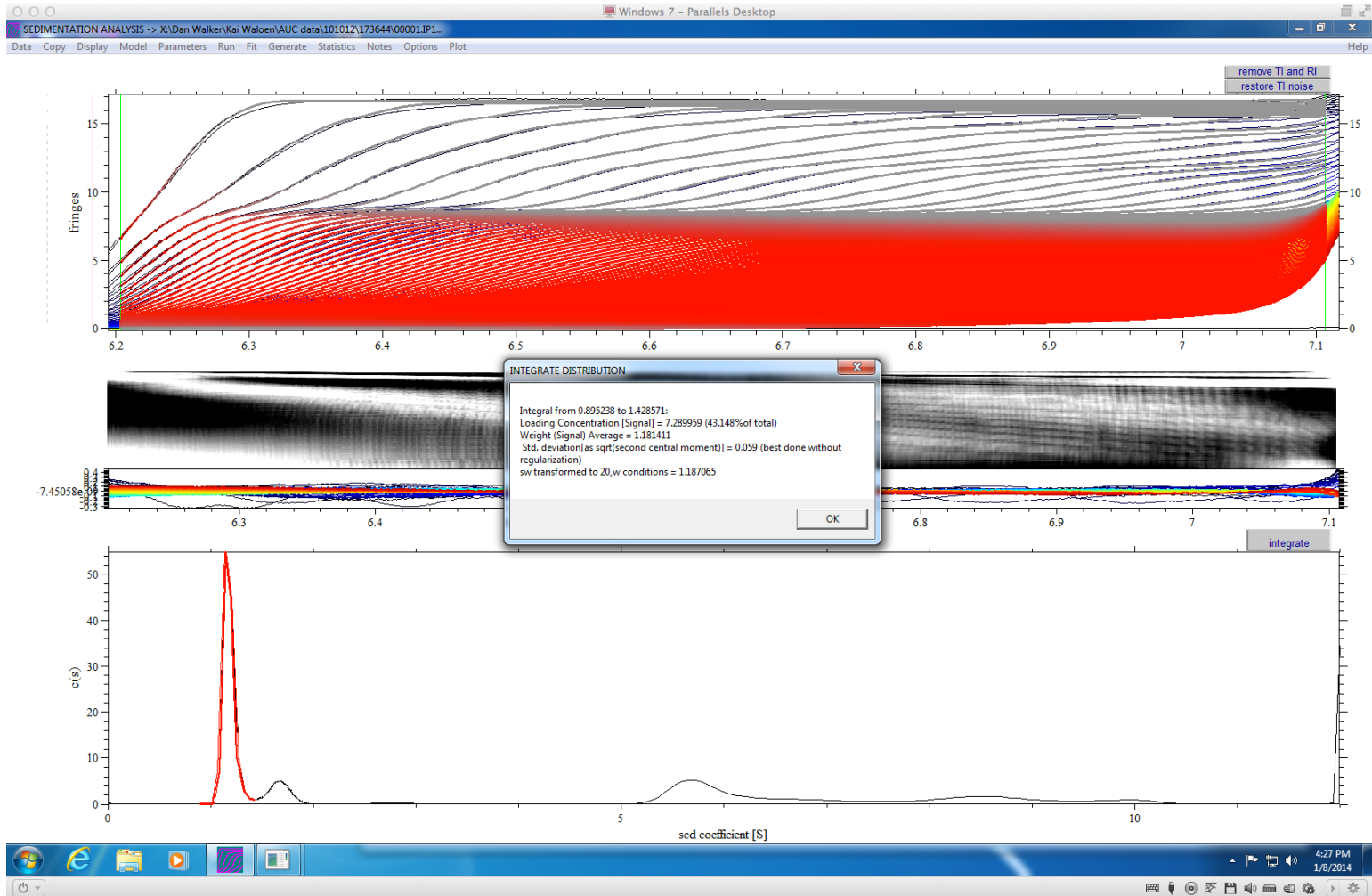
# Sum of Lamm equations $0 \leq s \leq 12$ S discretised by 200



Truncating upper fit limit does not increase the resolution at lower s

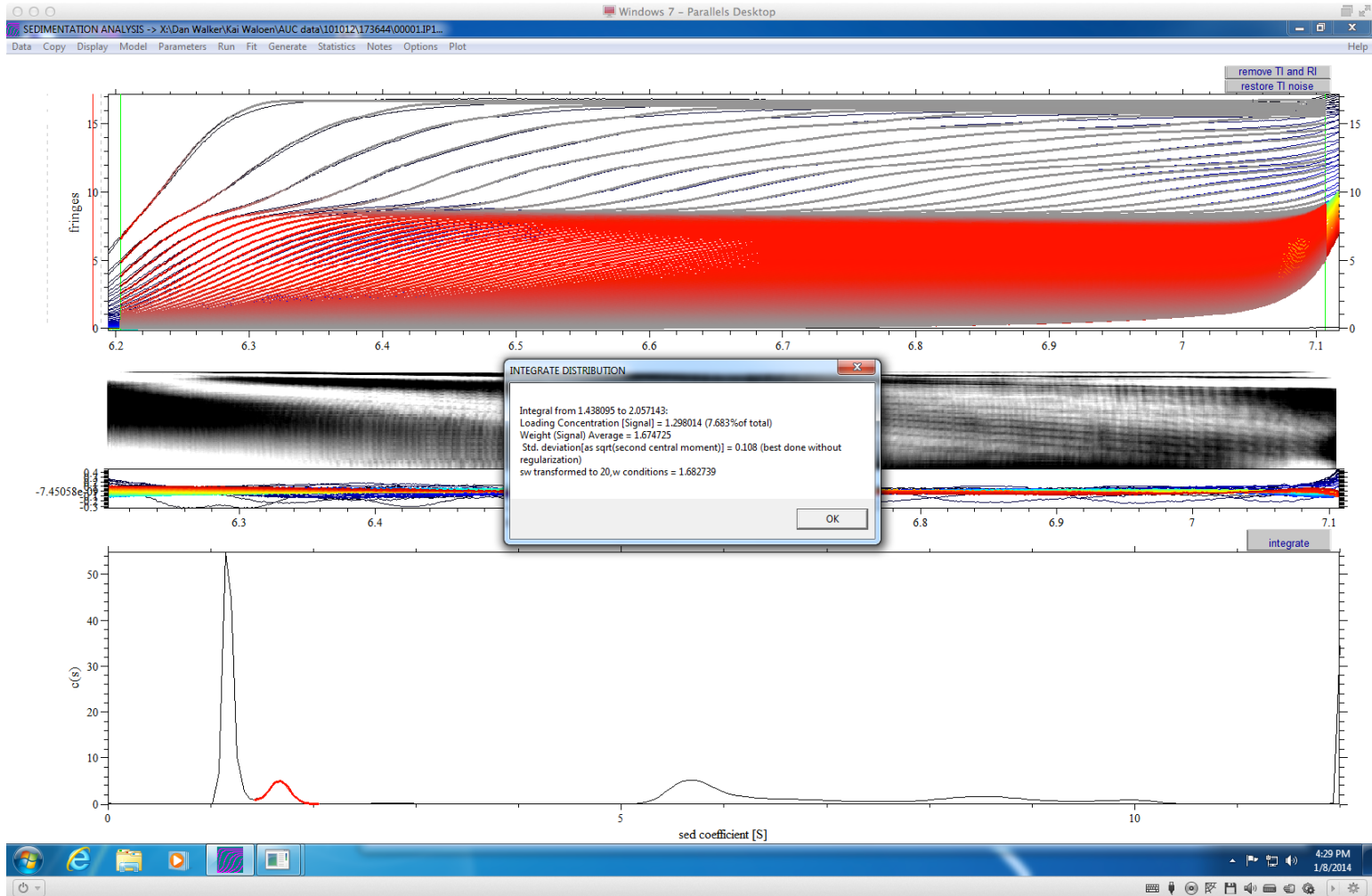


# Integrating $c(s)$ peaks reveals region of boundary that contains species

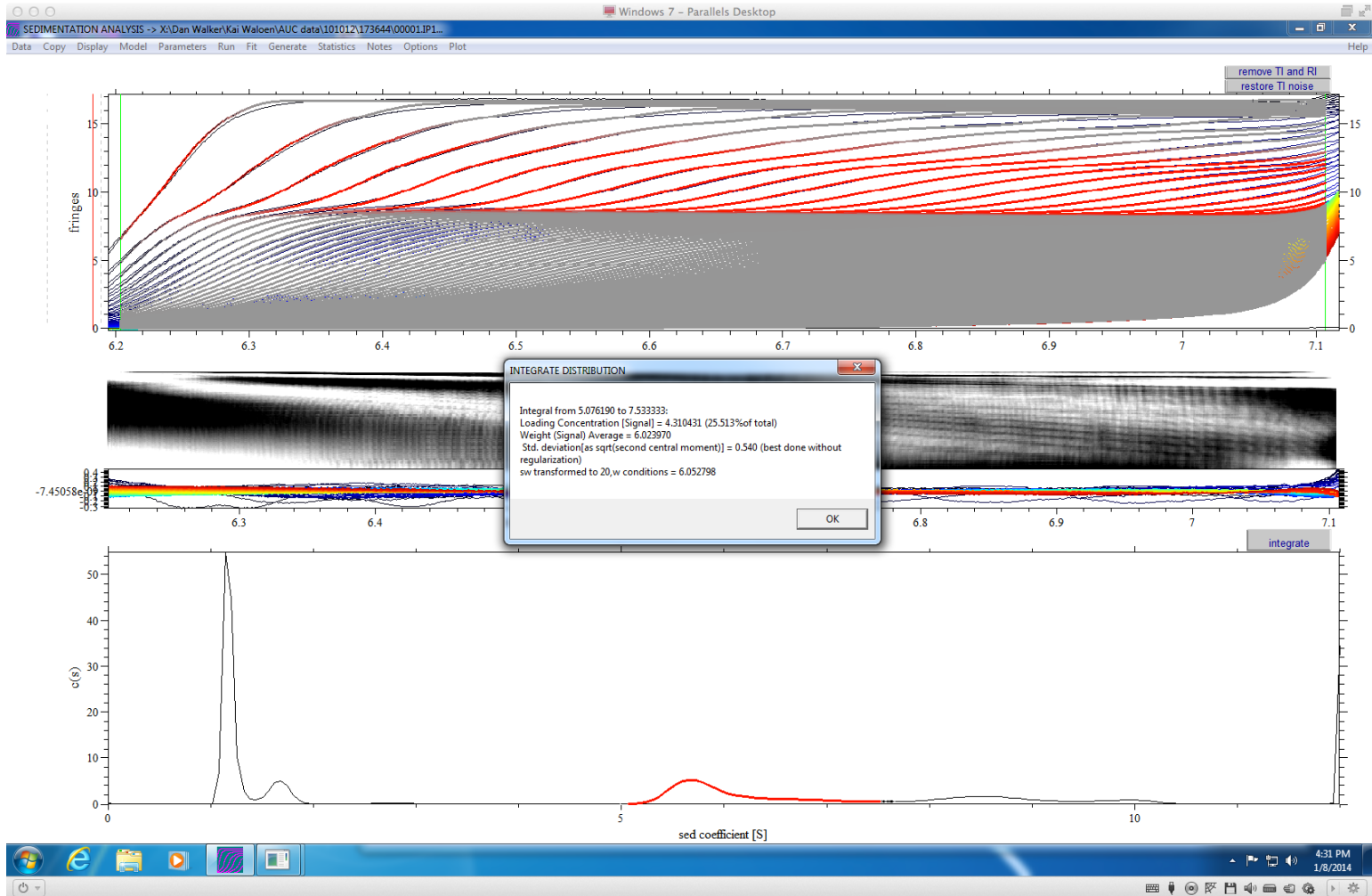




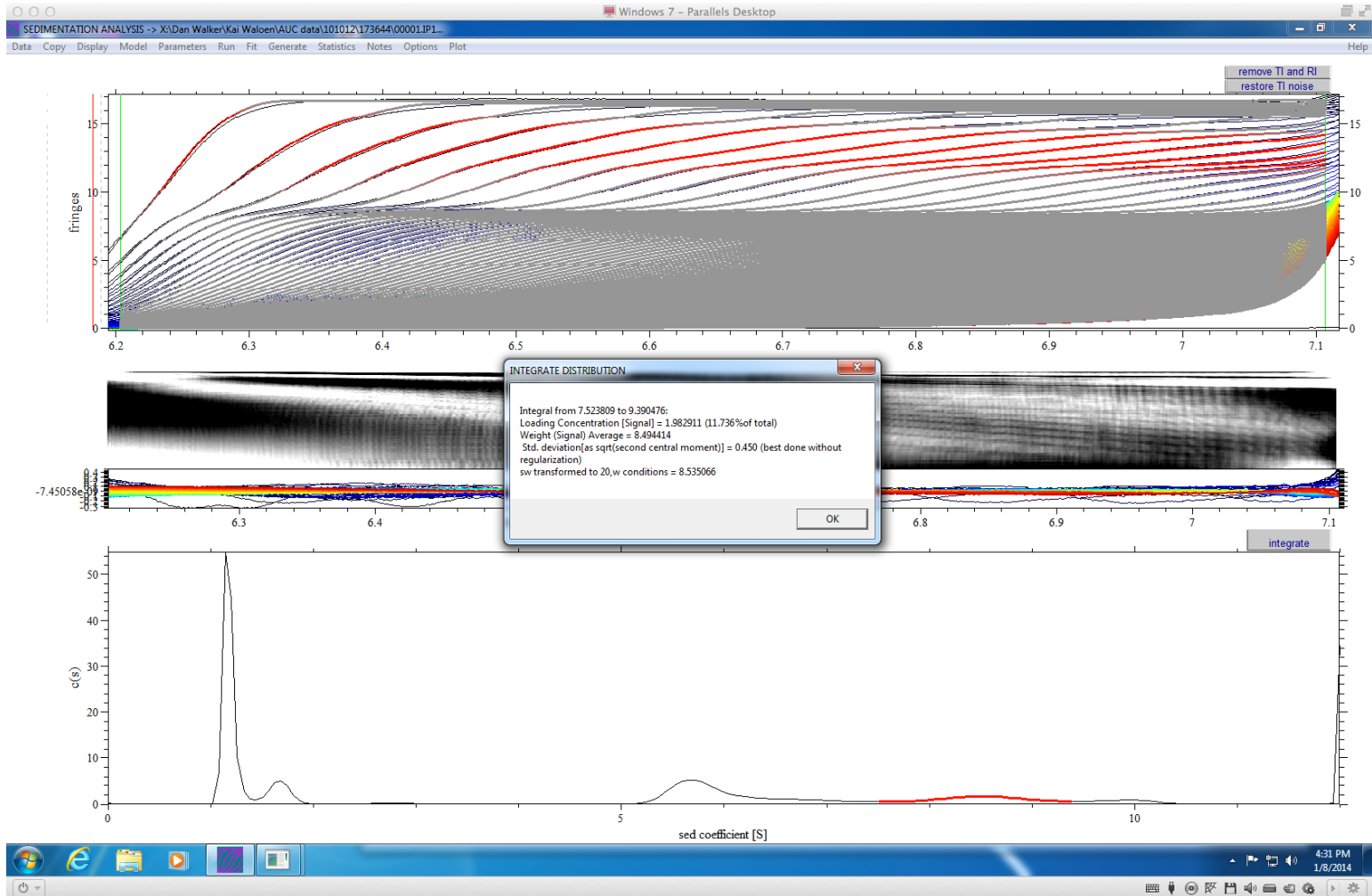
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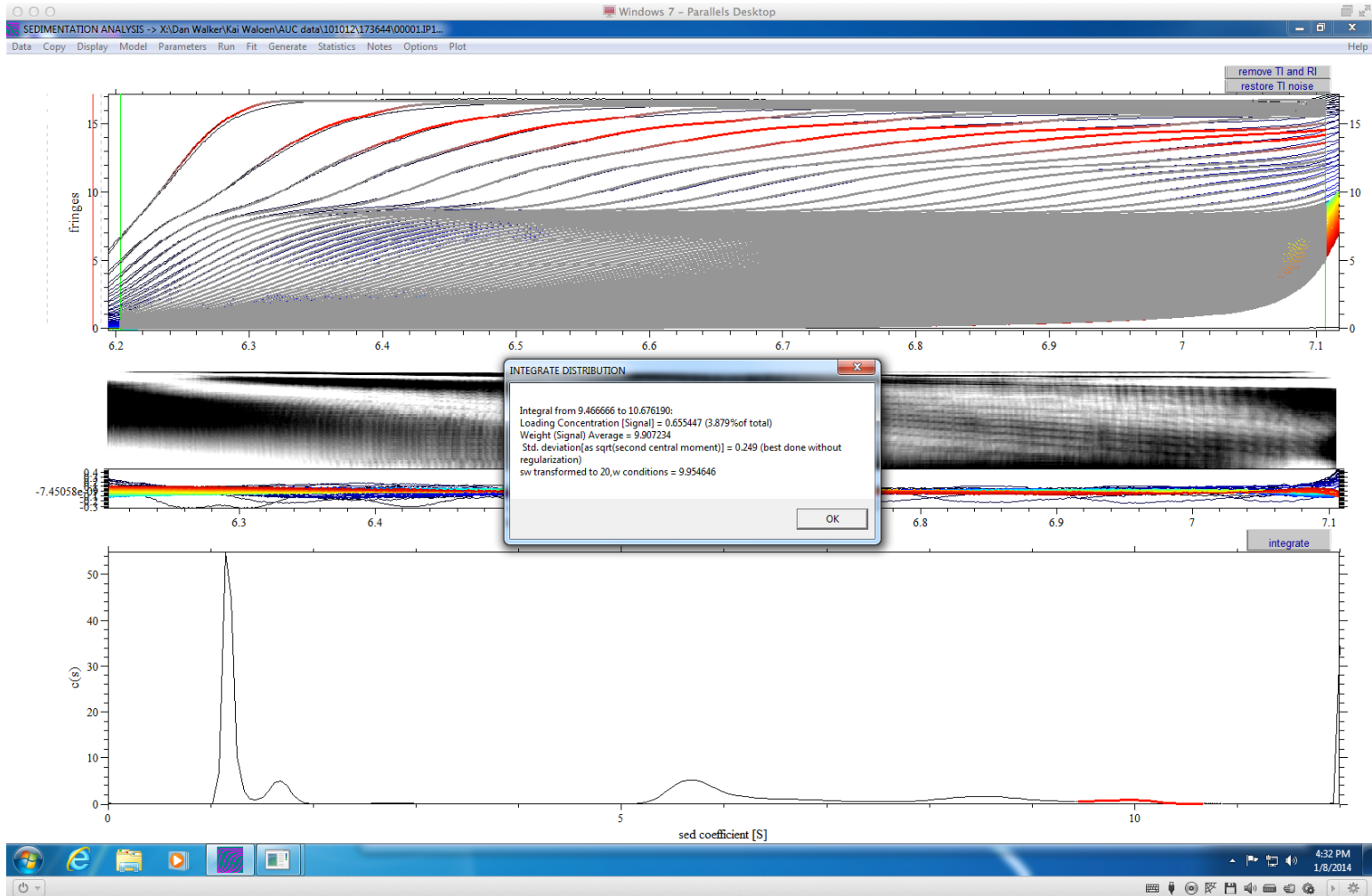
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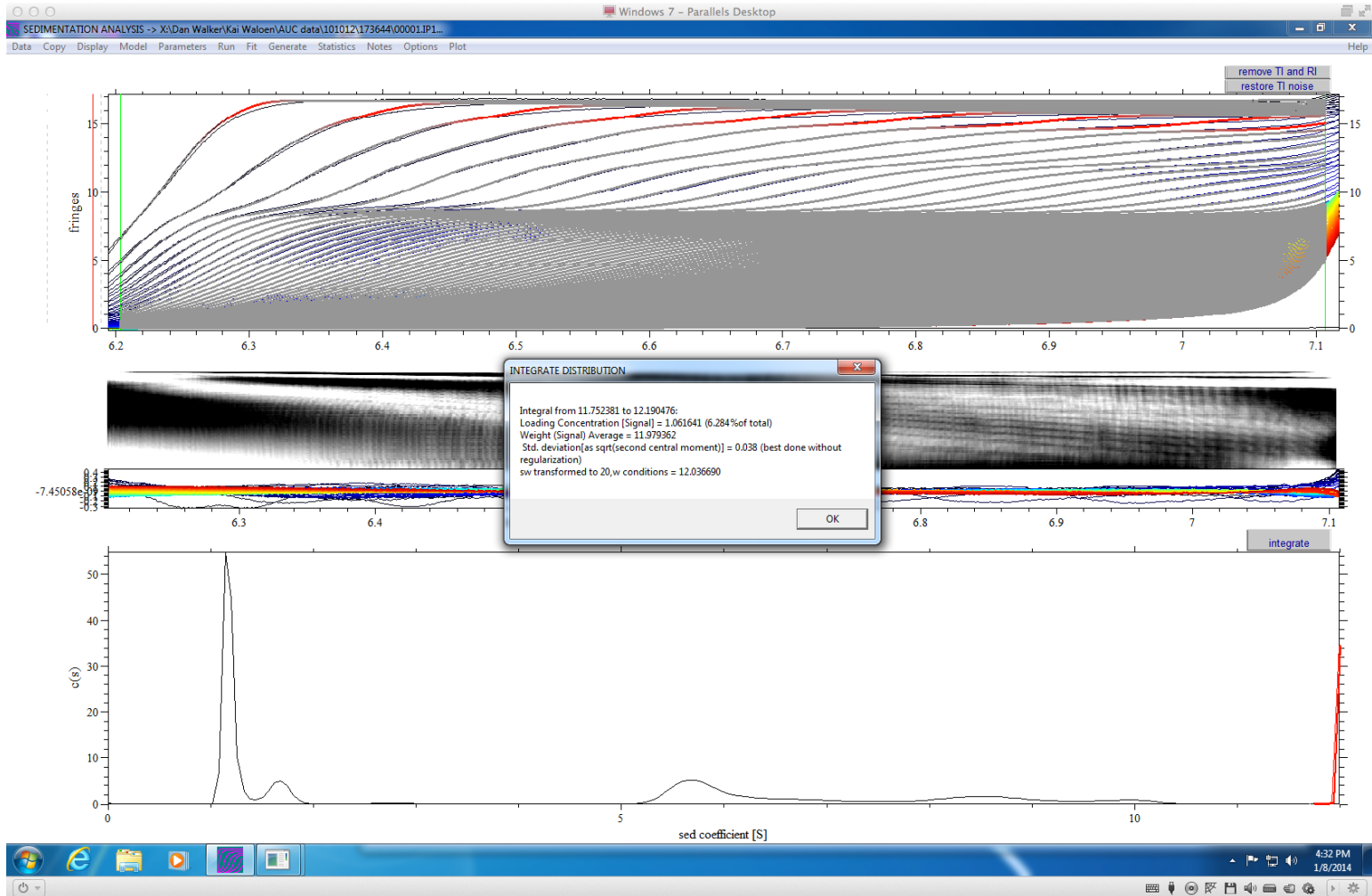
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# Integrating c(s) peaks reveals region of boundary that contains species



# Self association: SE data are the sum of exponentials

$$A_r = \exp[\ln A_0 + \text{H.M}(r^2 - r_0^2)] \leftarrow \text{monomer}$$

$$+ \exp[n_2 \ln A_0 + \ln K a_2 + n_2 \cdot \text{H.M}(r^2 - r_0^2)]$$

$\leftarrow 1-n_2$

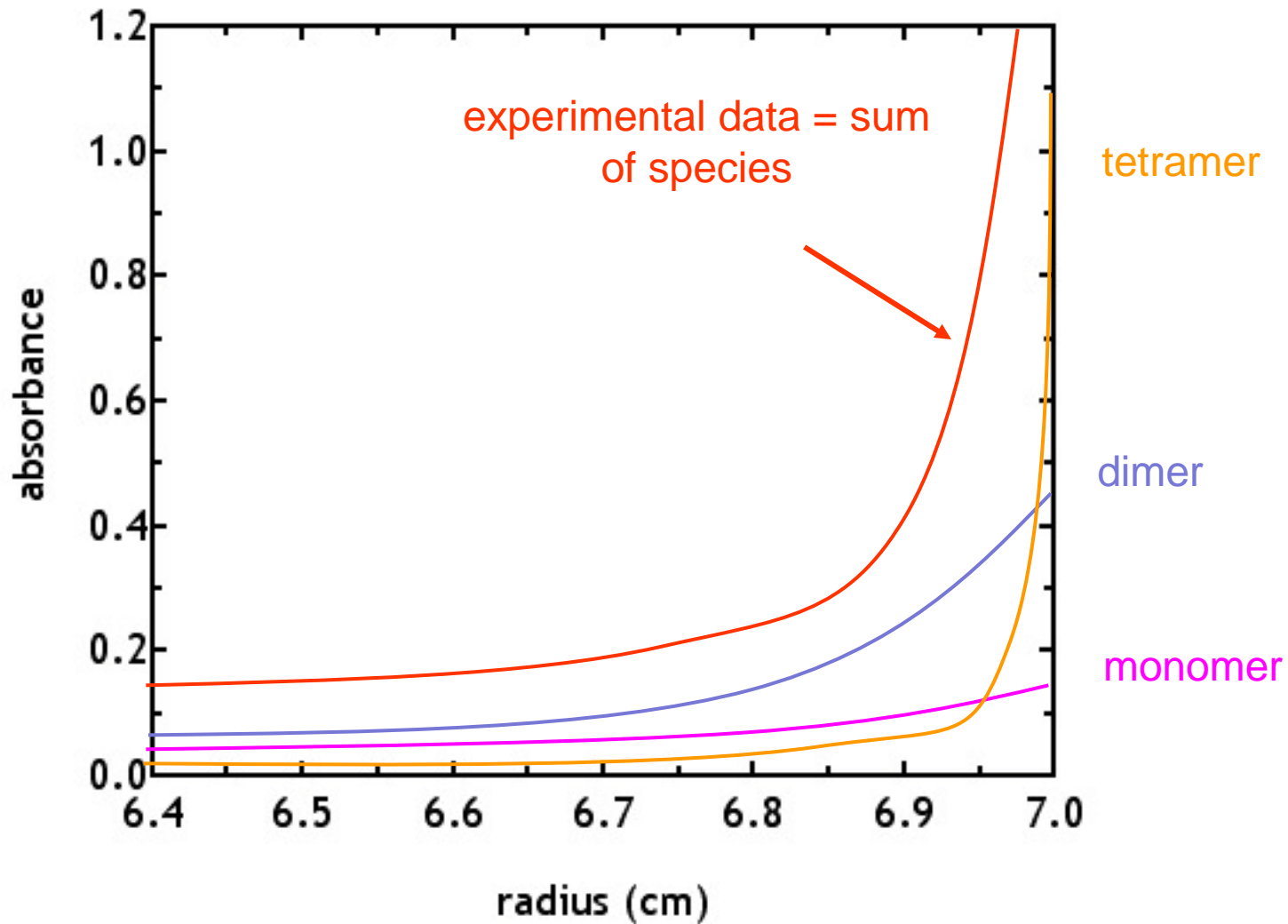
$$+ \exp[n_3 \ln A_0 + \ln K a_3 + n_3 \cdot \text{H.M}(r^2 - r_0^2)]$$

$\leftarrow 1-n_3$

$$+ \exp[n_4 \ln A_0 + \ln K a_4 + n_4 \cdot \text{H.M}(r^2 - r_0^2)] + E$$

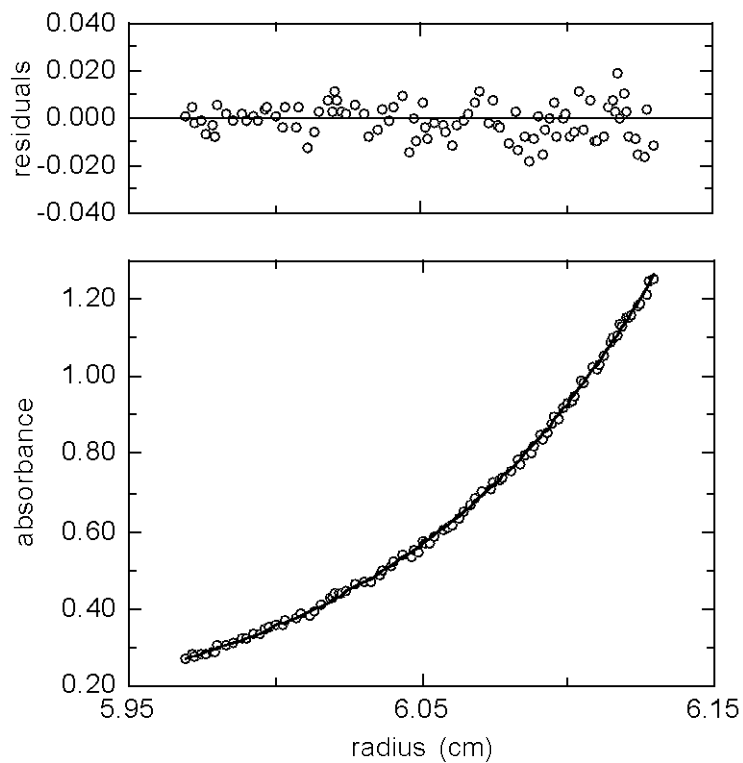
$\leftarrow 1-n_4$

# Self-association: “deconvolution” into individual components

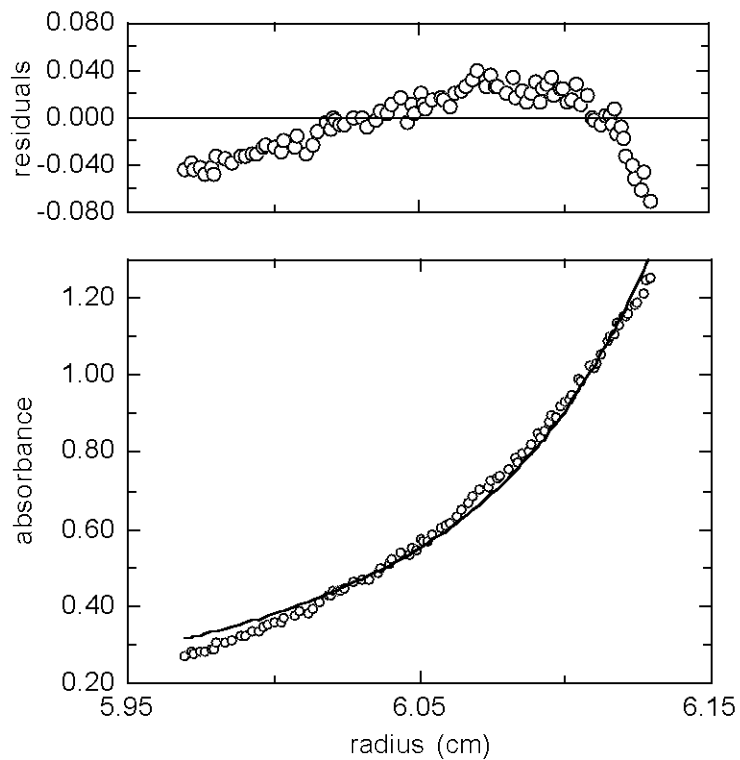


# Self-association: best model revealed by residuals

2-4



1-4





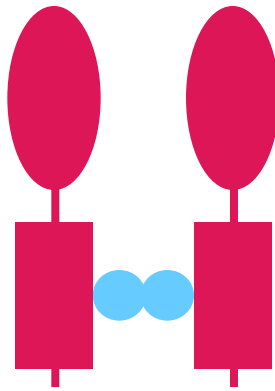
**LET'S HAVE A BREAK!**

# Outline

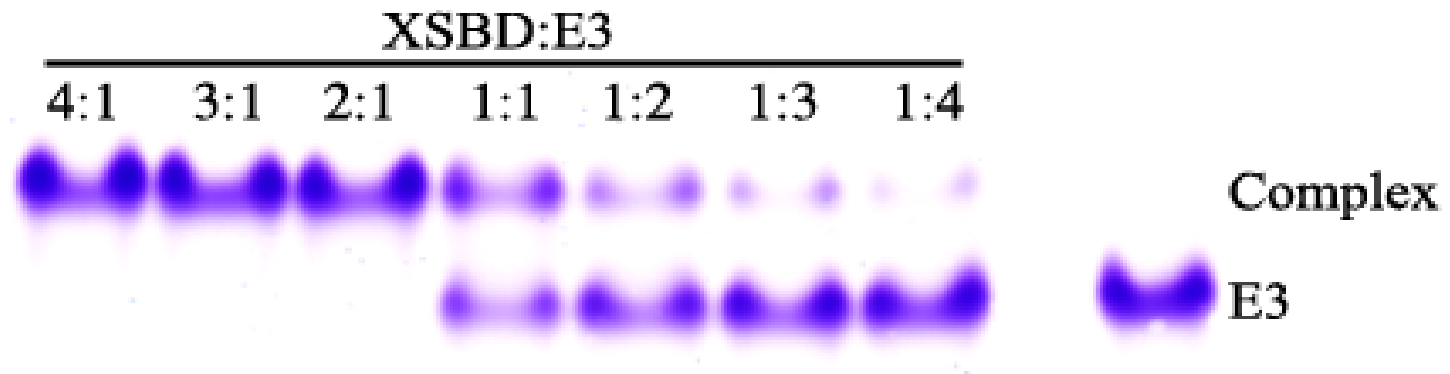
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# Hetero-association example: PDC E3BP-DD:E3 sub-complex

- E3 forms a homo-dimer
- E3 binds to E3BP-DD

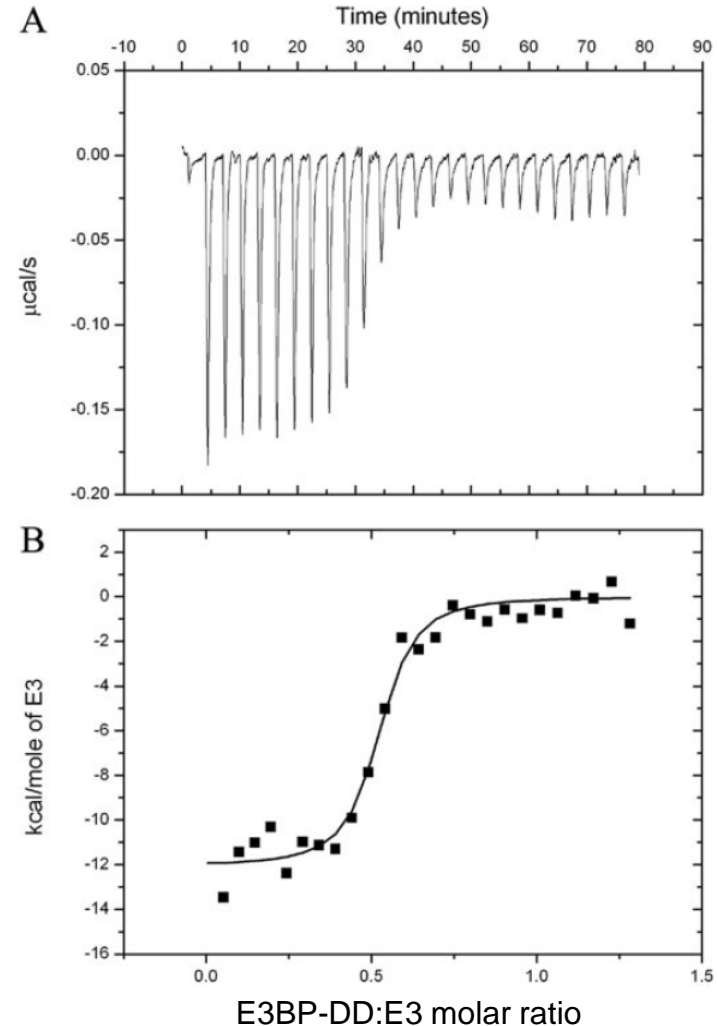


# Native PAGE: stoichiometry is 2:1



# ITC: stoichiometry is 2:1

- Microcal VP-ITC
- $T = 25^{\circ}\text{C}$
- Proteins dialysed o/n vs ref buffer
- 10  $\mu\text{l}$  aliquots E3 (40.7  $\mu\text{M}$ ) titrated into 6.2  $\mu\text{M}$  E3BP-DD
- Data fitted with non-linear regression model (Microcal software)
  
- $K_d = 36 \text{ nM}$
- $\Delta H = -12.1 \text{ kcal/mol}$
- $T\Delta S = -1.7 \text{ kcal/mol}$
- $N = 0.5$  molecules E3 bind/molecule E3BP-DD
  - equivalent to 2 E3BP-DD/E3

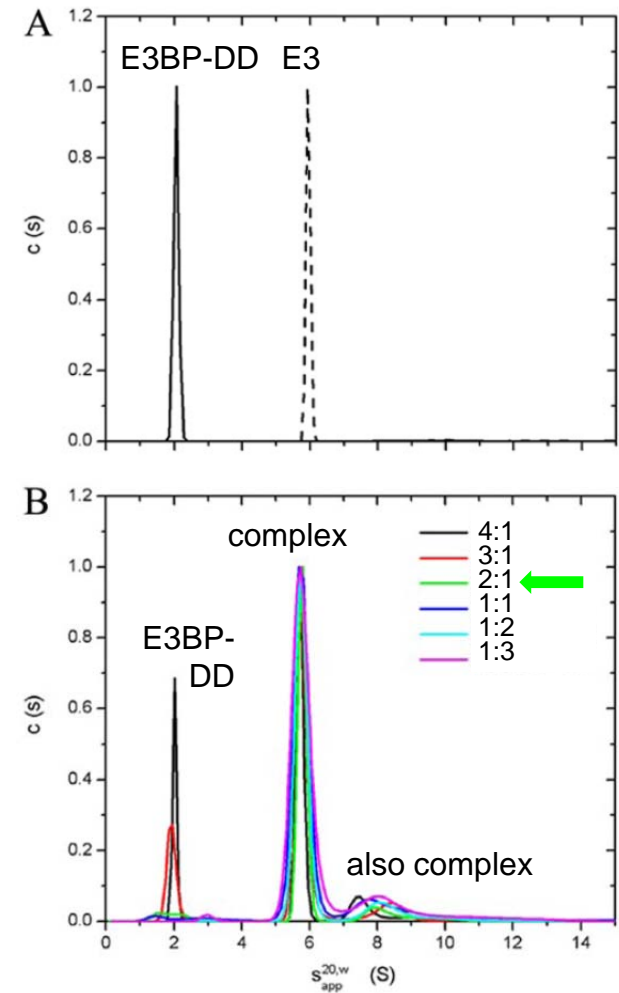


# SV titration

- $T = 4^{\circ}\text{C}$ 
  - Must ensure that  $T$  is constant
  - Takes *hours* to thermally equilibrate
- Rotor speed 45k rpm
- Interference optics used
  - Scan interval 1 minute
- $[\text{E3}] = 4.9 \mu\text{M}$
- Sample volume 380  $\mu\text{l}$
- Pathlength 12 mm

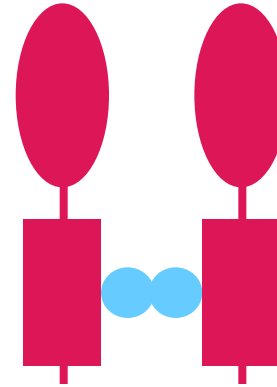
# SV titration: stoichiometry is 2:1

- Expt 1: SV of E3 alone; SV of E3BP-DD alone
  - Determine their  $s$
- Expt 2: SV of E3BP-DD+E3
  - At what ratio does E3BP-DD peak vanish?
  - This reveals stoichiometry: 2:1
  - Note 2 complex peaks
    - Different conformations
      - $s \approx 6$  S peak less compact
      - $s \approx 8$  S peak more compact



# SE titration

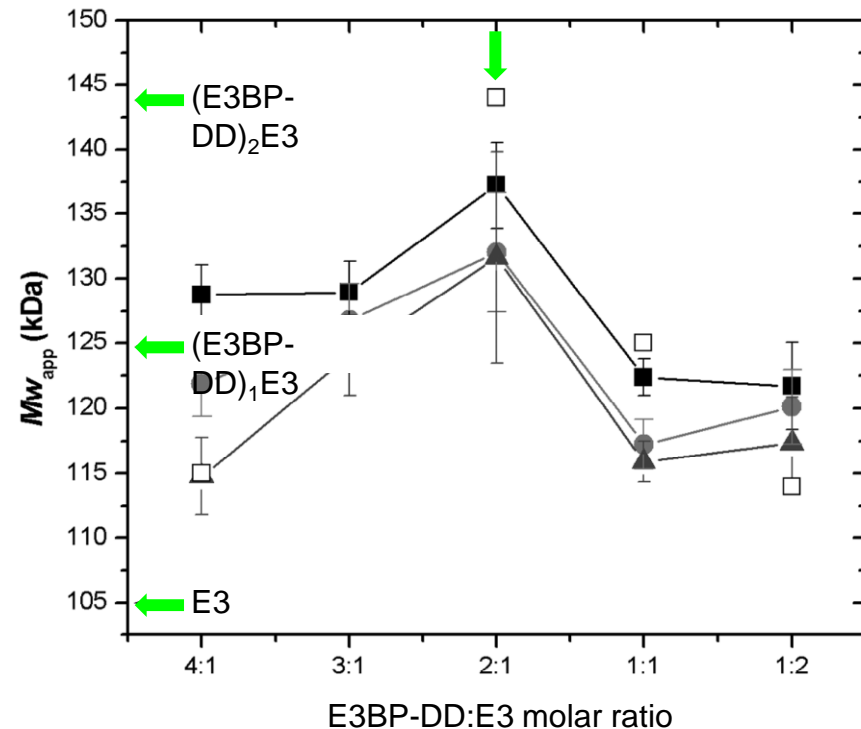
- From amino acid sequence:
  - E3BP-DD M = 19.5 kDa
  - E3 M = 105 kDa
- Sample volume = 30  $\mu$ l
- Path-length 3 mm
- SE performed at 3 rotor speeds
  - 8.5, 12, 16k rpm
    - Appropriate for different complexes
- Absorbance data (280 nm)
- Radial step size 0.001 cm
- Program WINMATCH used to demonstrate attainment of equilibrium
  - Comparison of scans 3 h apart





# SE titration: stoichiometry is 2:1

- Whole-cell weight-average  $M$  ( $M_{w,app}$ ) determined
  - e.g. using species analysis in SEDPHAT with 1 species only
  - No model assumed
- When E3BP-DD is in excess
  - $M_{w,app} < M_{complex}$  until complex is formed
- When E3 is in excess
  - $M_{w,app} < M_{complex}$  because excess E3 lowers  $M_{w,app}$
- ??? Why  $M_{w,app} \neq M_{complex}$  at 2:1???



# Outline

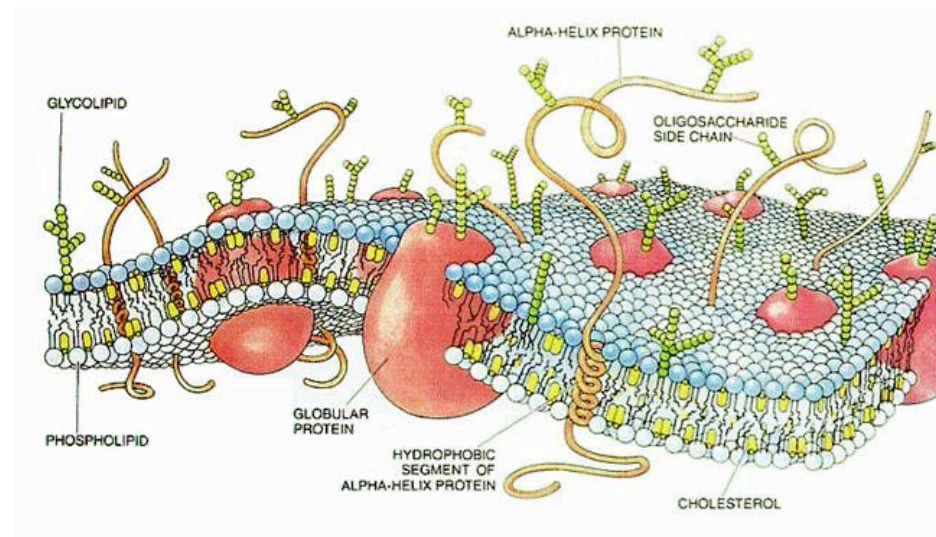
- AUC background
- How AUC experiments are performed
- Data analysis
- Example: simple model-independent investigation of a hetero-association
- **Detergent solubilised systems**
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# Detergent solubilised proteins: density matching SE

- In SE bouyant molecular weight is determined:

$$M_p(1 - \phi' \rho) = M_p[(1 - \bar{v}_p \rho) + \delta_{\text{Det}}(1 - \bar{v}_{\text{Det}} \rho)]$$

- In many AUC expts we want to observe self-association
- Density matching is a good method for self-associating membrane proteins



Burgess, N. K., Stanley, A. M. & Fleming, K. G. (2008). Determination of membrane protein molecular weights and association equilibrium constants using sedimentation equilibrium and sedimentation velocity. In *Methods in Cell Biology* (J. Correia & H. W. Detrich, III, eds.), **84**, 181-211. Academic Press

# Density matching SE: experimental conditions

- Experimental conditions adjusted such that:
  - solvent  $\rho$  = effective  $\rho$  of bound detergent

$$\rho = 1/\bar{v}_{\text{Det}}$$

$$M_p(1 - \phi'\rho) = M_p[(1 - \bar{v}_p\rho) + \delta_{\text{Det}}(1 - \bar{v}_{\text{Det}}\rho)]$$

0

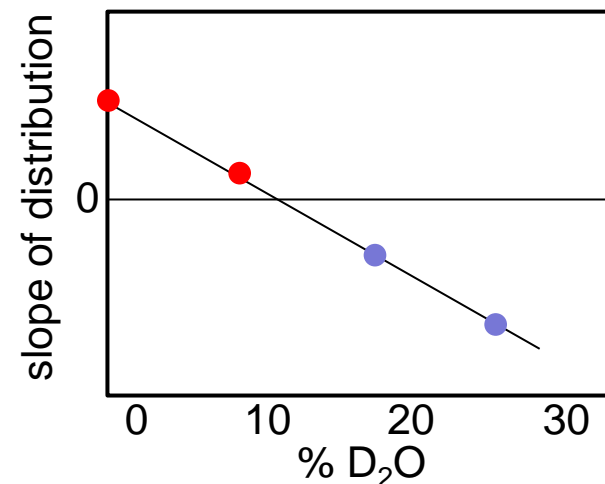
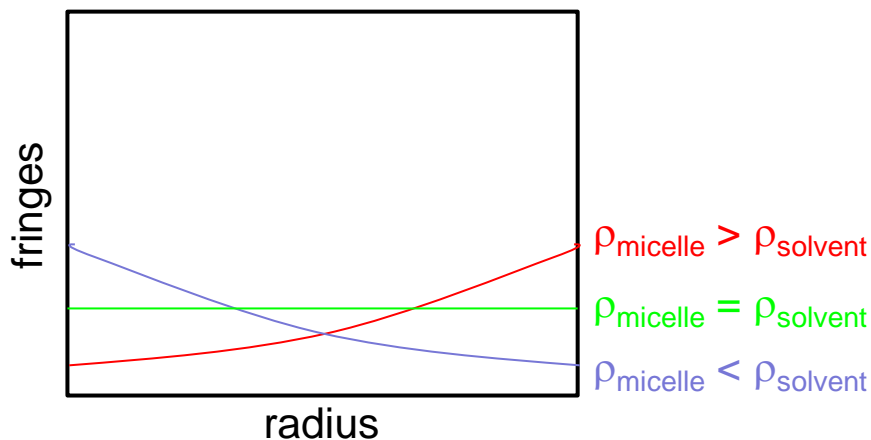
- So detergent becomes effectively invisible to centrifugal field
- SE data can be analysed with standard methods

# BUT.....this method works only in certain conditions

- The solvent density must be adjusted with D<sub>2</sub>O or D<sub>2</sub><sup>18</sup>O
  - Alternatives would be e.g. sucrose or other co-solvent
  - Affect chemical potential
  - Lead to preferential binding and/or exclusion of water or additional co-solvent at protein surface
- But use of D<sub>2</sub>O or D<sub>2</sub><sup>18</sup>O limits detergents that can be used
  - $\rho \bar{v}_{D_2O} = 1.1 \text{ g/ml}$
  - of the  $\bar{v}_{\text{detergent}}$  must be between that of water and D<sub>2</sub>O
  - i.e.  $0.9 \leq \bar{v} \leq 1.0 \text{ ml/g}$
  - Eliminates:
    - dodecylmaltoside ( $\rho = 1.21 \text{ g/ml}$ ,  $\bar{v} = 0.83 \text{ ml/g}$ )
    - $\beta$ -octylglucoside ( $\rho = 1.15 \text{ g/ml}$ ,  $\bar{v} = 0.87 \text{ ml/g}$ )
  - Suitable:  $\bar{v}$ 
    - C8E5 ( $\bar{v} = 0.993 \text{ ml/g}$ )
    - C14SB (density matched by 13% D<sub>2</sub>O in 20 mM Tris-HCl, 200 mM KCl)
    - Dodecylphosphocholine (DPC, density matched by 52.5% D<sub>2</sub>O in 50 mM Tris-HCl, 100 mM NaCl)

# Determination of density-matching point for C14SB

- Determine % of D<sub>2</sub>O required to density match C14SB micelles in background of other buffer components
  - 30 mM C14SB in 20 mM Tris-HCl, 200 mM KCl made in 0, 10, 20, 30% D<sub>2</sub>O
  - Reference solvent the same minus detergent
  - SE observed with interference optics
    - Collect “buffer blanks” for subtraction to reduce noise
    - Then replace buffer with micelle solution in sample channel
    - Rotor speed 50k rpm
    - T = 25°C



# SE of systems solubilised by C14SB: OMPLA

- Outer membrane phospholipase A (OMPLA)
  - Gram negative bacteria
- Beckman XL-A, T = 25°C
- 20 mM Tris-HCl, 200 mM KCl
- 13% D<sub>2</sub>O
  - [OMPLA] = 0.3, 0.6, 0.9 A<sub>280</sub> (12 mm pathlength)
  - Rotor speed = 16.3, 20, 24.5k rpm
  - [C14SB] = 5 mM
  - Increased [detergent] → dilution of protein that is solubilised in detergent phase thus promoting dissociation
  - Monomer mass determined



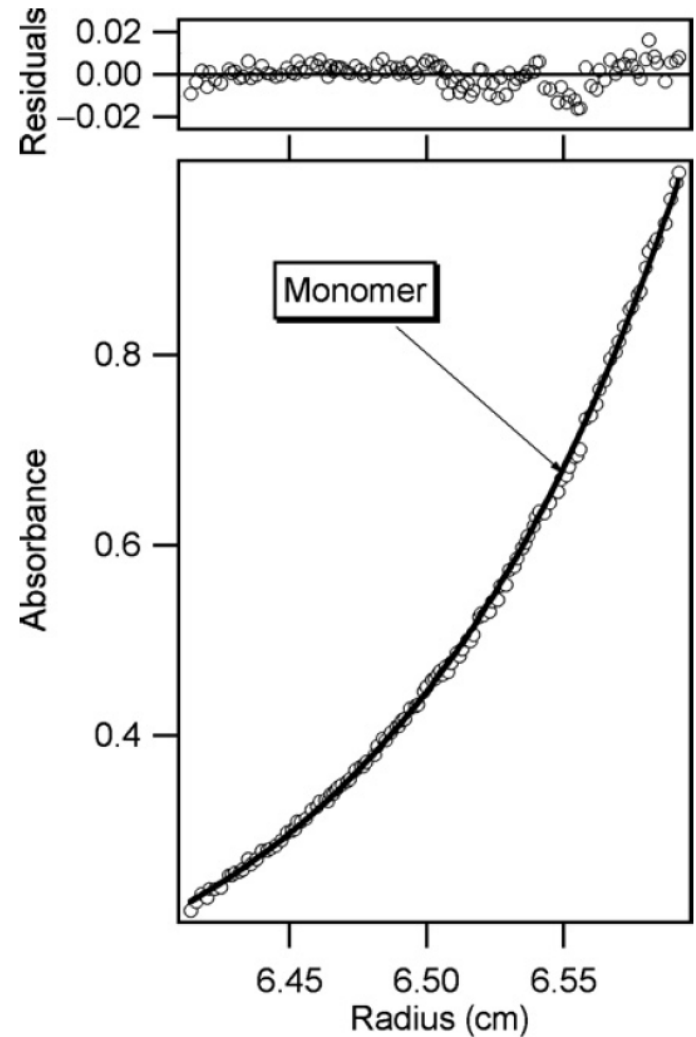
# OMPLA studied at 3 concs, 3 rotor speeds for each of 4 conditions

1. OMPLA
2. OMPLA + 20 mM  $\text{CaCl}_2$
3. OMPLA + covalently bound fatty acyl chain substrate analogue
4. OMPLA + covalently bound fatty acyl chain substrate analogue + 20 mM  $\text{CaCl}_2$



# SE results: 1. OMPLA

- SE data first globally fitted with equation for single ideal species
- Good fits
  - $\sqrt{\sigma^2} \approx$  instrument noise ( $\approx 0.005$ )
  - Residuals randomly distributed about 0
- M for all 9 data sets within 5% of monomer M
- Conclusion: OMPLA monomeric in absence of co-factors

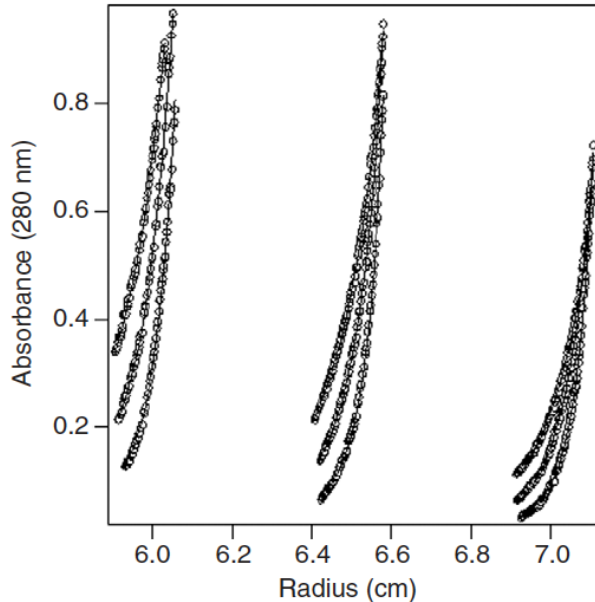
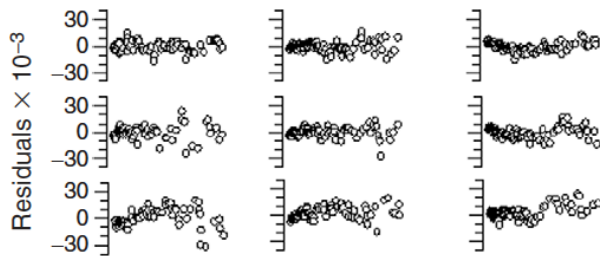


## SE results: 4. OMPLA + covalently bound fatty acyl chain substrate analogue + 20 mM CaCl<sub>2</sub>

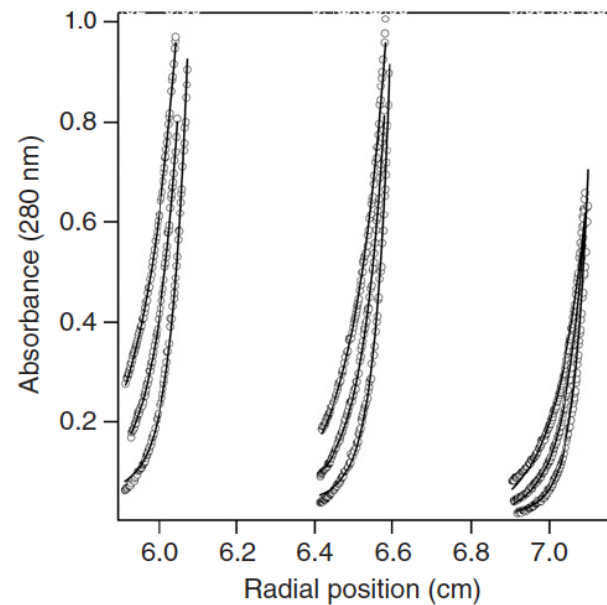
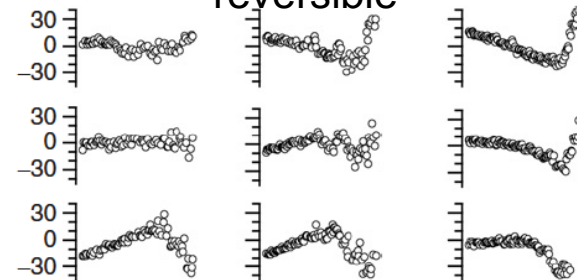
- 2 fatty acyl chain analogues tested:
  - decylsulfonylfluoride (DSF)
  - perfluorinated octylsulfonylfluoride (pOSF) (all H replaced by F)
- For both analogues, single species fits returned  $M > M_{\text{monomer}}$
- Therefore tried
  - Monomer-dimer
  - Monomer-trimer
  - Monomer-tetramer
- Fitting parameter is  $K_d$

# OMPLA-DSF reversibly dimerises

DSF: monomer-dimer reversible



pOSF: monomer-dimer not reversible



# SE of systems solubilised by C14SB: OmpF

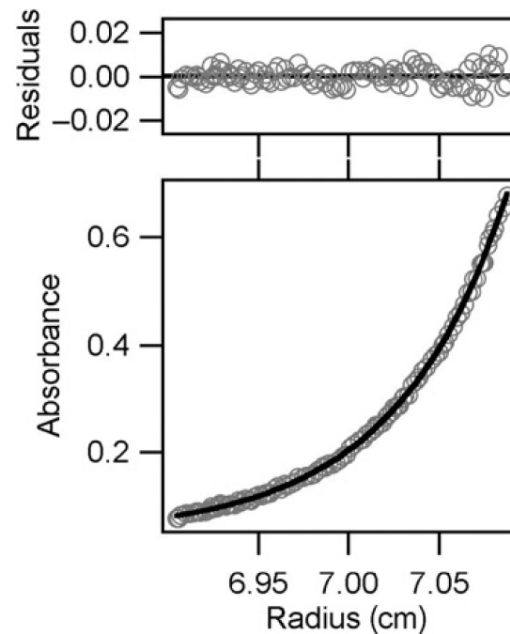
- *E. coli* OmpF
- Beckman XL-A, T = 25°C
- 20 mM Tris-HCl, 100 or 200 mM KCl
- 13% D<sub>2</sub>O
- OmpF normally trimer
- Collected 36 data sets:
  - [OmpF] = 0.3, 0.6, 0.9 A<sub>230</sub> (12 mm pathlength)
  - [C14SB] = 5, 12 & 30 mM
  - Rotor speed = 9, 11, 13.5, 16.3k rpm



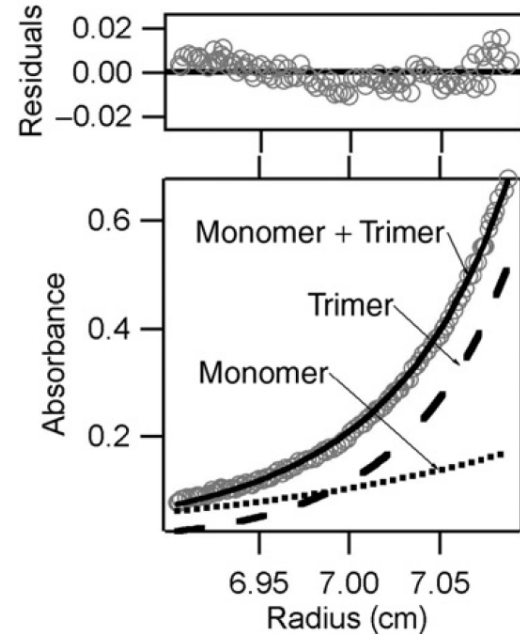
# OmpF

- Self-association probed in 2 ways:
  - Working at low [protein]
  - Increasing [detergent]
- At each [detergent], SE data globally fitted
  - For 4 rotor speeds & 3 [protein]

A Single-ideal trimer



B Monomer/trimer equilibrium

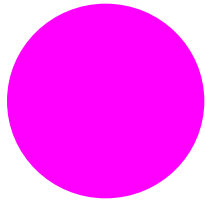


# Outline

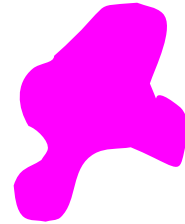
- AUC background
- How AUC experiments are performed
- Data analysis
- Example: simple model-independent investigation of a hetero-association
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- **Hydrodynamic bead modelling (HBM)**
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$s$  = deviation from sphericity + hydrodynamic hydration

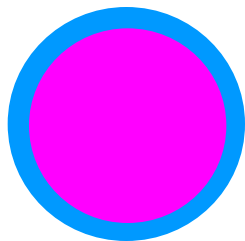
$$s = \frac{M(1 - \bar{v}\rho)}{N_A f}$$



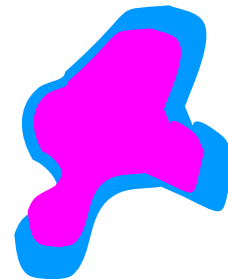
$M, f_0$



$M, f > f_0$

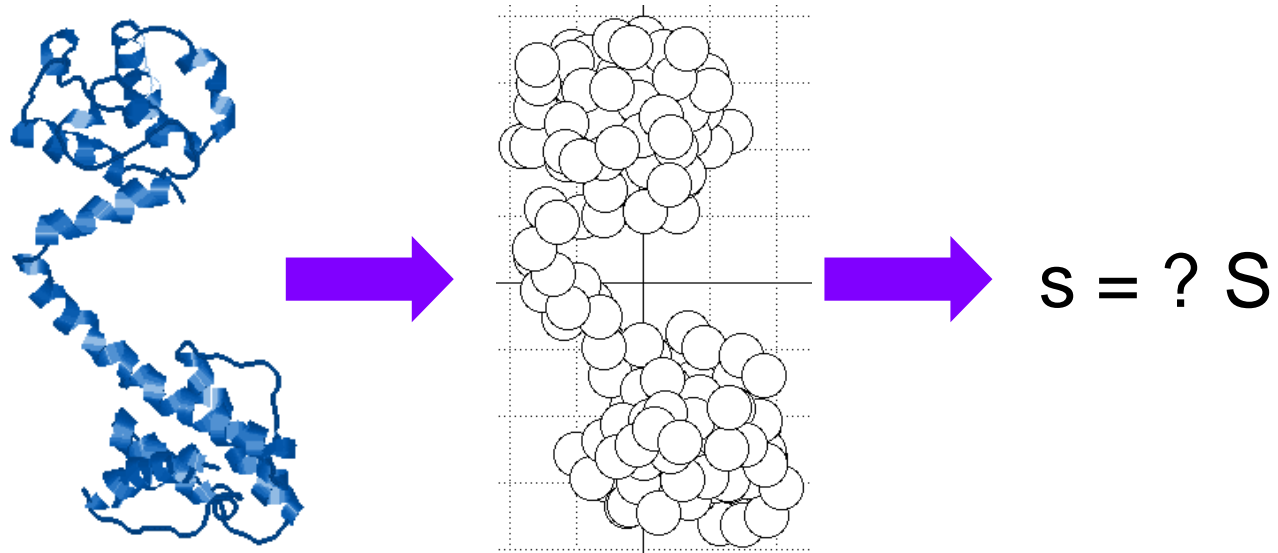


$M, f > f_0$



$M, f \gg f_0$

# Sedimentation coefficient is a constraint for SAS modelling



- For one sphere  $f_0 = 6\pi\eta R_0$
- For an assembly of N spheres an approximate solution is

$$f_t = \frac{\sum_{i=1}^N \zeta_i}{1 + (6\pi\eta_0 \sum_{i=1}^N \zeta_i)^{-1} \sum_{i \neq j}^N \sum_j^N \zeta_i \zeta_j r_{ij}^{-1}}$$

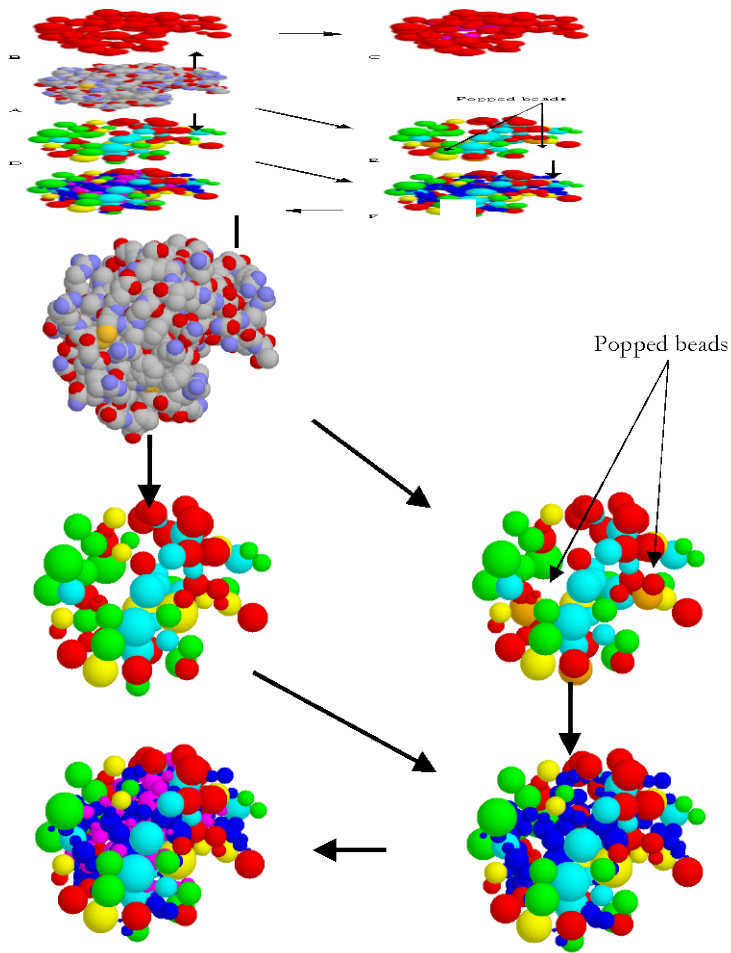
- where  $\zeta_i = 6\pi\eta_0\sigma_i$



# Several freely available programs for HBM

- A more exact expression for  $f_t$  together with expressions for other hydrodynamic and related parameters are encoded in HBM software:
- José García de la Torre *et al.* (Universidad Murcia, Spain)
  - <http://leonardo.inf.um.es/macromol/programs/programs.htm>
  - HYDRO
    - Computes hydrodynamic & other parameters for any bead model
  - HYDROPRO
    - Computes hydrodynamic & other parameters for models constructed from pdb files
  - And many other programs....
- Mattia Rocco, Emre Brookes
  - <http://somo.uthscsa.edu/>
    - Generates HBMs from pdb files, computes hydrodynamic & other parameters with realistic hydration

# SOMO - construction of “intelligently” hydrated bead models from atomic coordinates



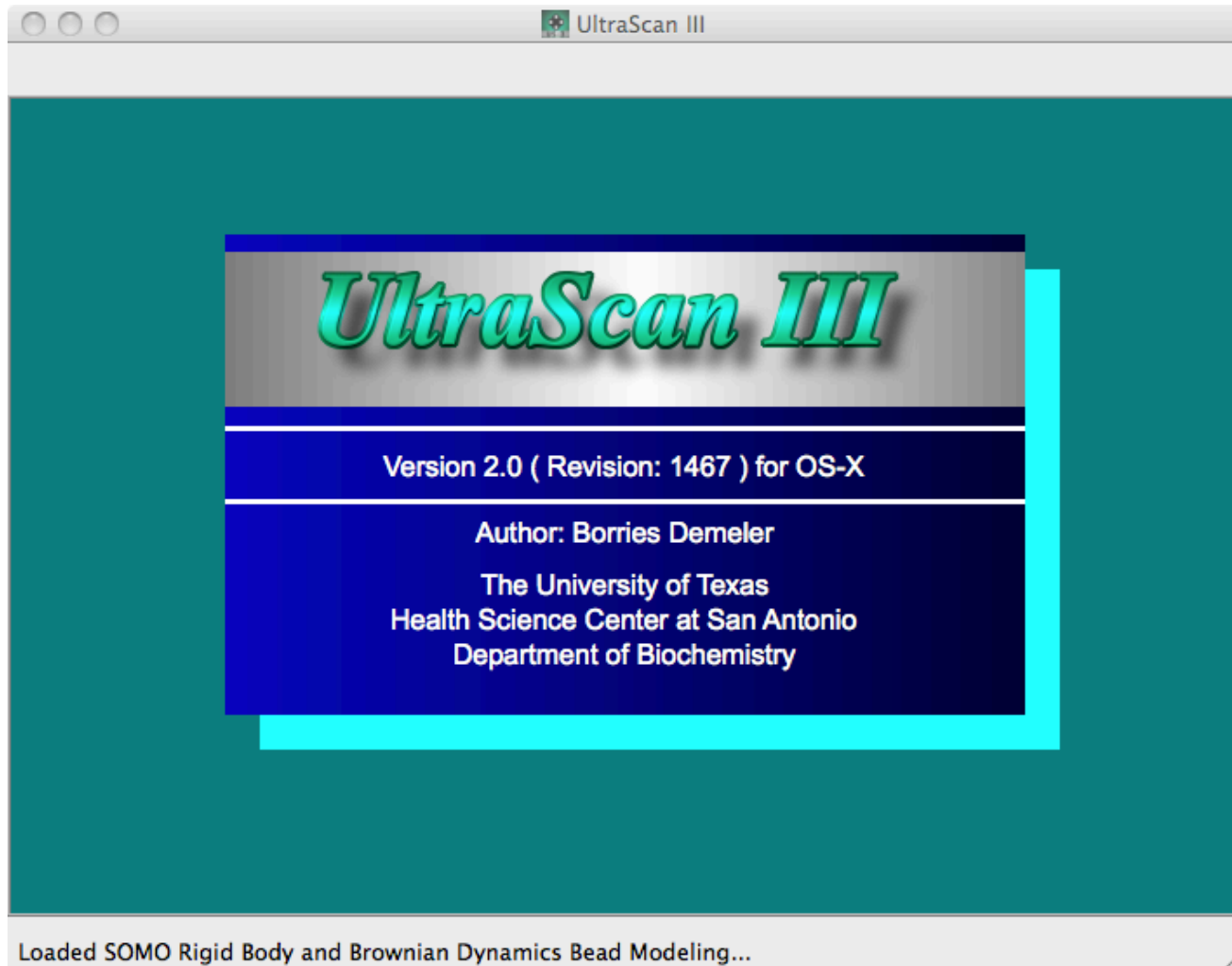
*AtoB*

*Trans*

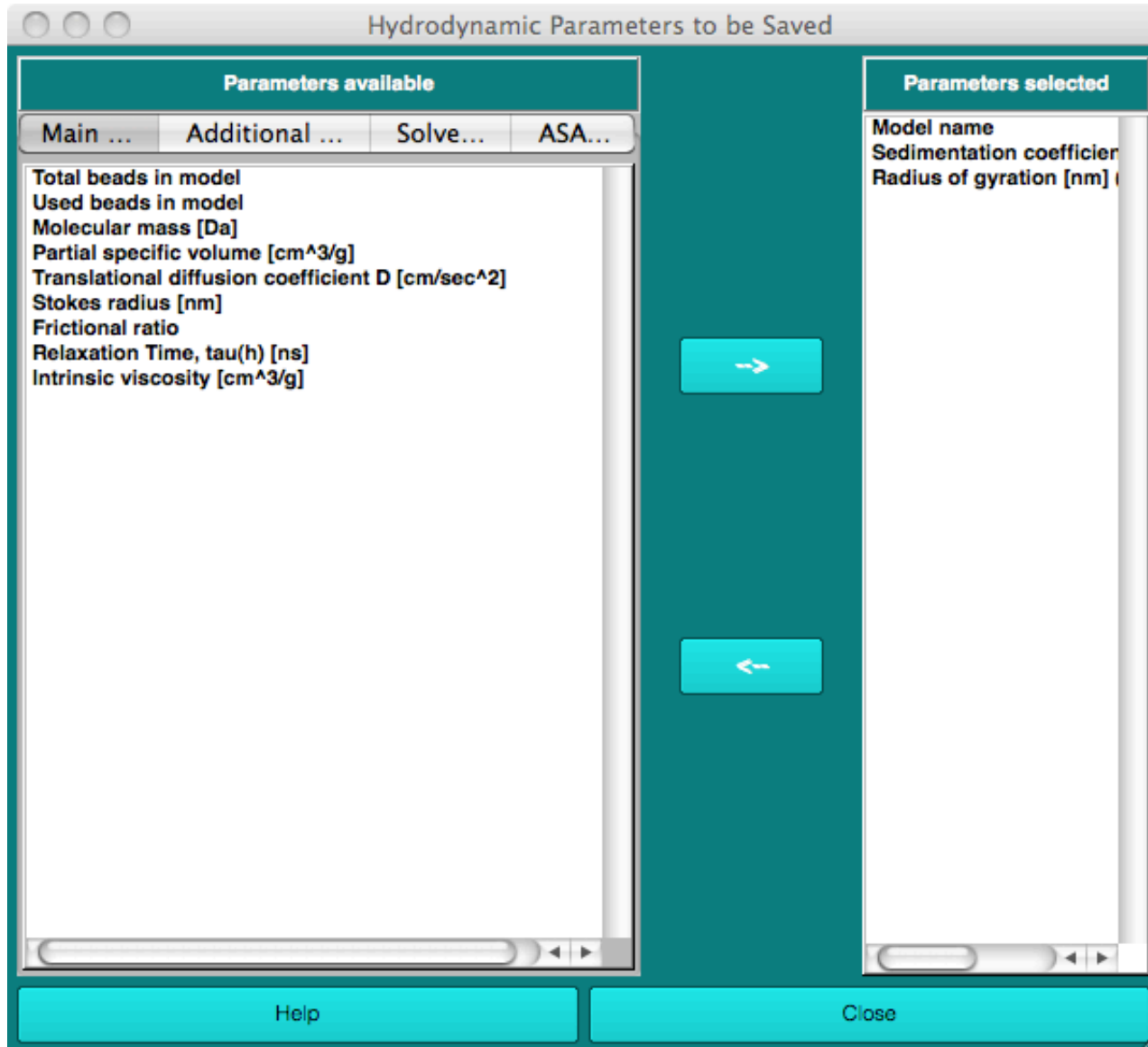
exposed acidic  
exposed basic  
exposed polar  
exposed  
nonpolar/hydrophobic  
mainchain  
buried

- Water of hydration included in each bead
- Bead overlaps removed hierarchically
  - Reducing radii + translating bead centres outwards
- Beads overlapping by > preset threshold are fused (“popped”)
- Buried beads excluded from hydrodynamic calculations
  - Reduces cpu time

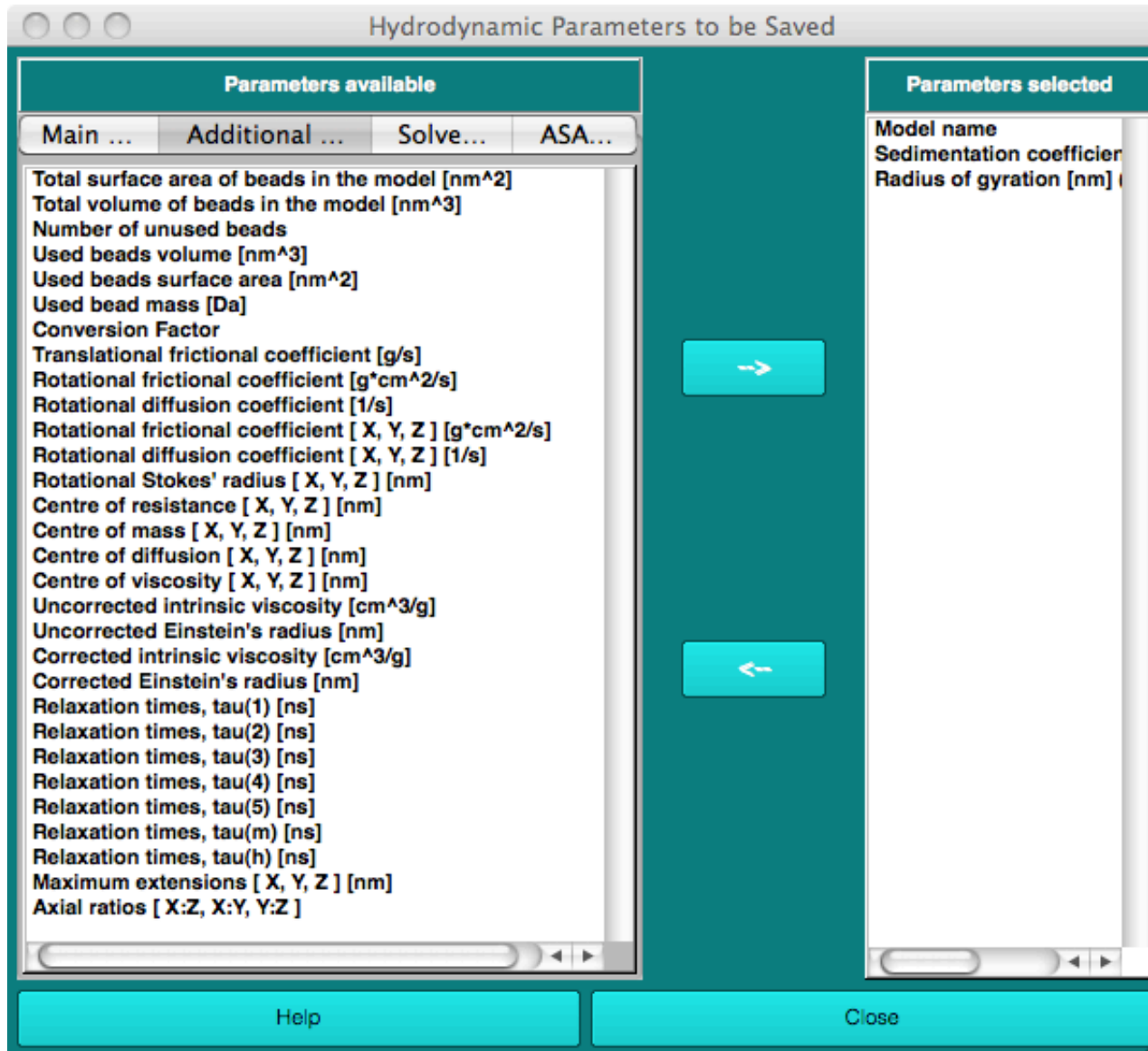
# SOMO is a subprogram of UltraScan III



# Parameters computed by SOMO (1)



# Parameters computed by SOMO (2)



# Outline

- AUC background
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# Example: Oligomerisation of synthetic polyvalent integrin $\alpha_5\beta_1$ ligands

- $\alpha_5\beta_1$  ligands used to immobilise cells on surfaces via
  - 9th type III FN domain synergy site (PHSRN)
  - 10th type III FN domain RGD site
- $\alpha_5\beta_1$  ligand oligomers facilitate increased binding
- Oligomerisation accomplished via 5 heptad repeats based on GCN4 leucine zipper
  - I/L placed variously @ a and d positions to promote di-, tri- & tetramerisation
- Thiol-linked immobilisation to surface achieved via C-terminal Cys
  
- Question: do the ligands oligomerise as designed?

# Construction of hydrodynamic bead models

MRGSHHHHHGMA**S**GLDSPTGIDFSDITANSFTVHWIAPRATITGYRIRHHPEHFSGRPREDRV**PHSRN**SIT  
LTNLTPGTEYVVSIVALNGREESPLIGQQSTVSDVPRDLEVVAATPTSLLISWDAPAVTVRYRITYGETG  
GNSPVQEFVPGSKSTATISGLKPGVDYTTITVYAVT**GRGD**SPASSKPISINYRTSKLEPKSSDTPPGSPRSP  
EPKSSDTPPGSPRSG**RIKQLEDKIEELLSKIYHLENEIARLKKLIGELEDKIENLGC**

↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

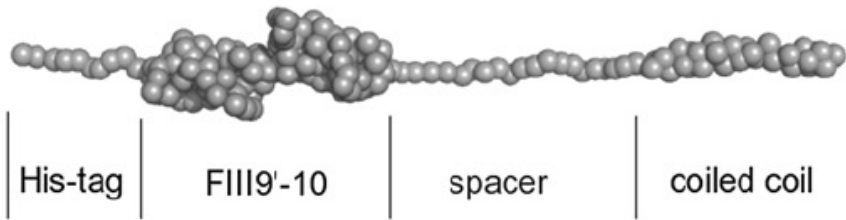
- From vector (including His-tag) – too short for e.g. SWISSMODEL
- FN III 9-10 domain pair homology model (SWISSMODEL)
- Synthesised “missing beads”
- Coiled-coil (42 a.a.) – SWISSMODELS generated for underlined segment



# Oligomer models generated

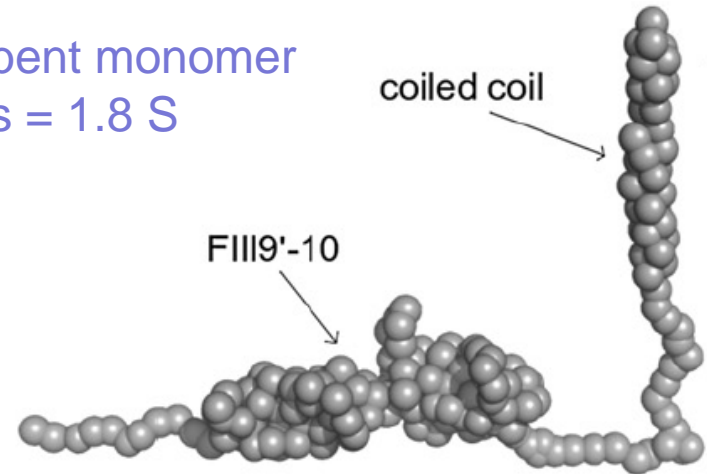
linear monomer  
 $s = 1.7 S$

A(i)



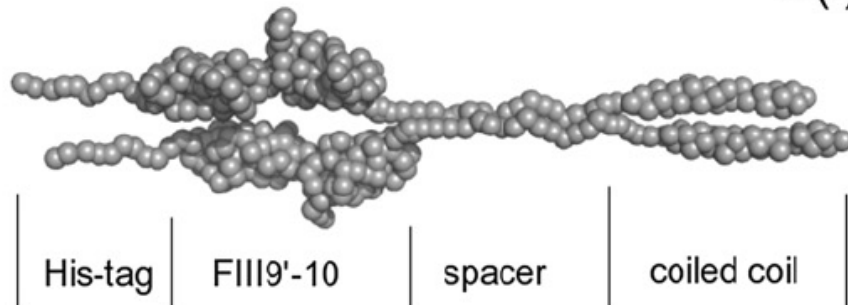
bent monomer  
 $s = 1.8 S$

A(ii)



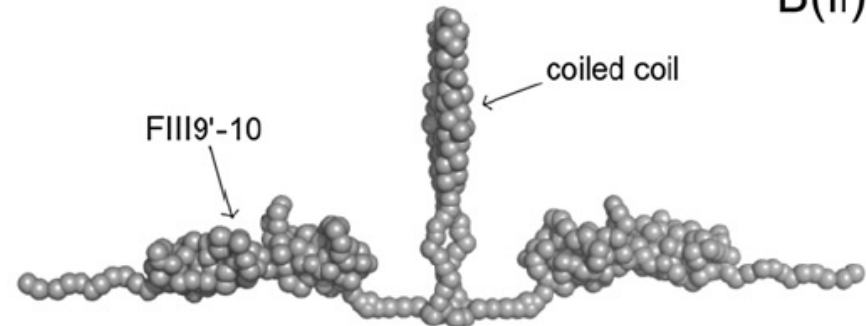
linear dimer  
 $s = 2.7 S$

B(i)



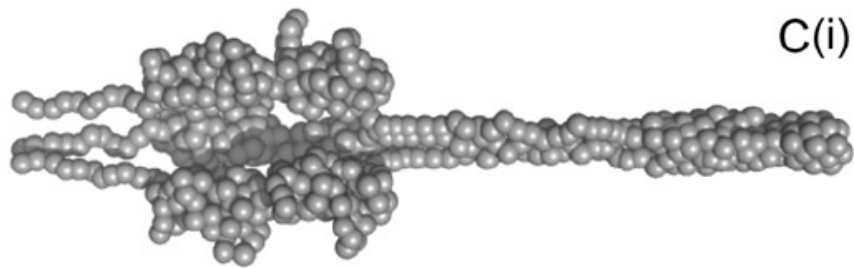
bent dimer  
 $s = 2.5 S$

B(ii)

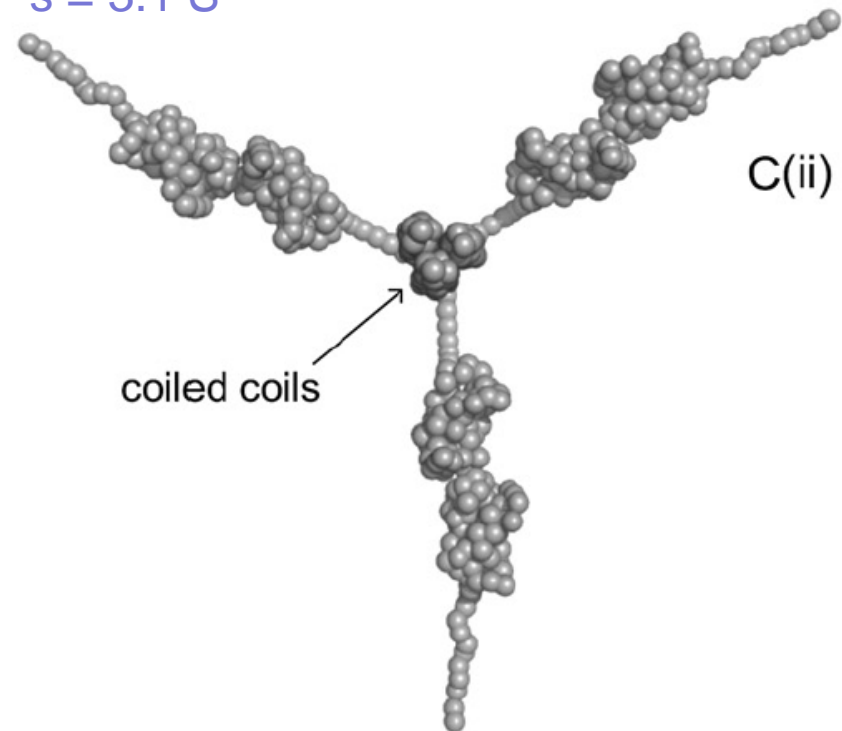


# Oligomer models generated

linear trimer  
 $s = 3.9 \text{ S}$

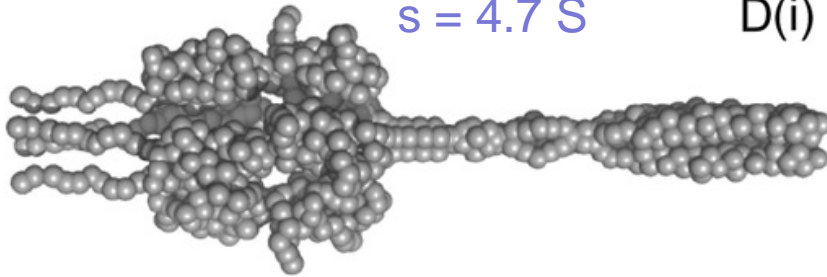


bent trimer  
 $s = 3.1 \text{ S}$

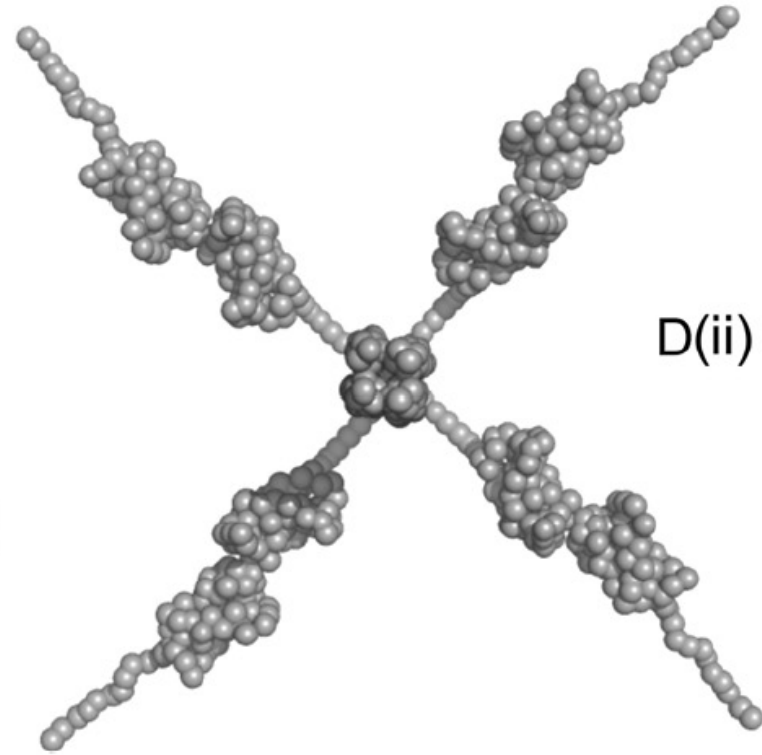


# Oligomer models generated

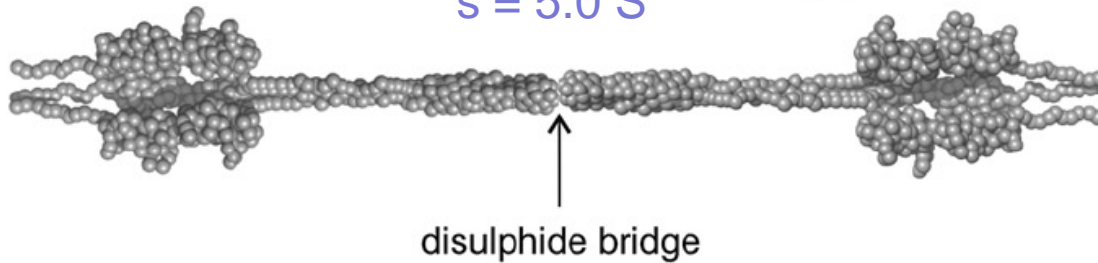
linear tetramer  
 $s = 4.7 S$  D(i)



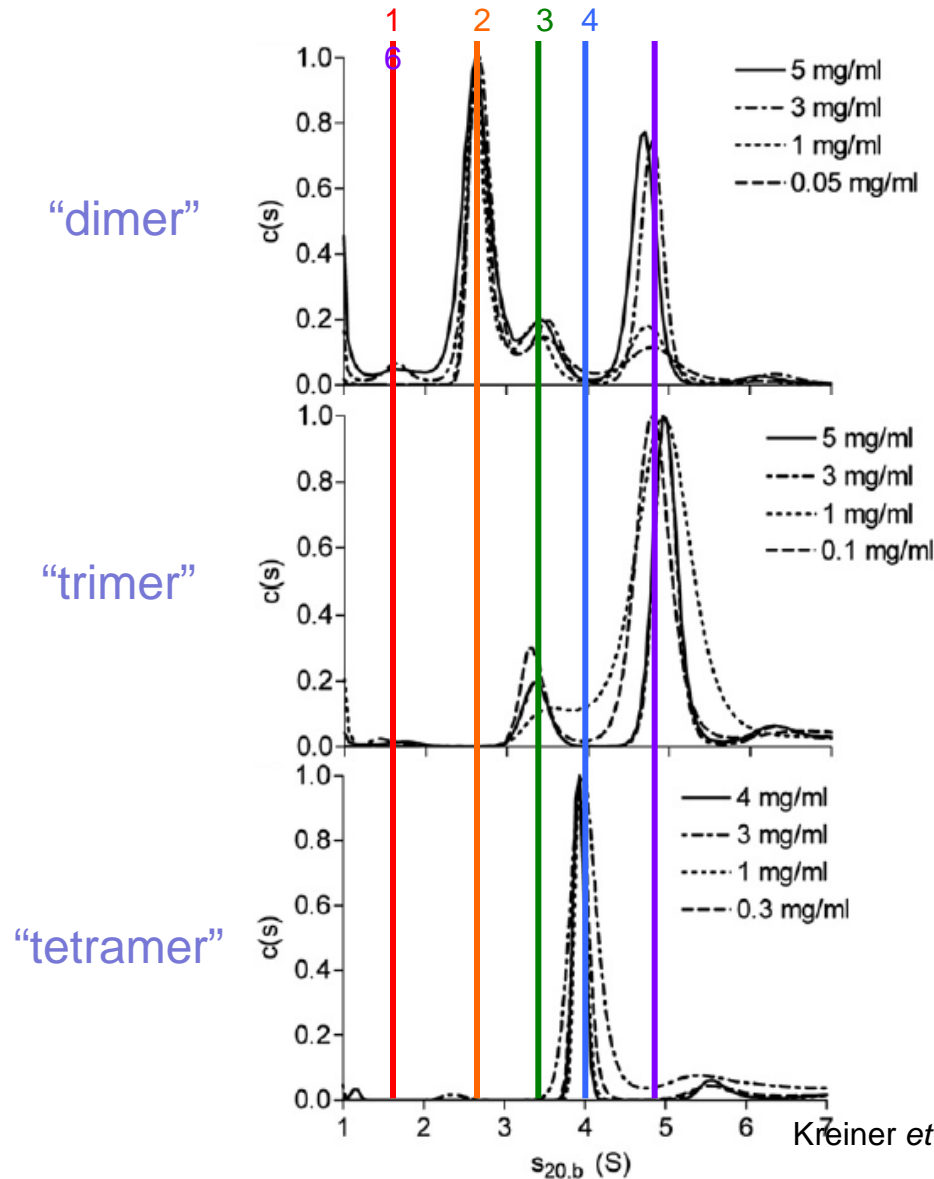
bent tetramer  
 $s = 3.7 S$  D(ii)



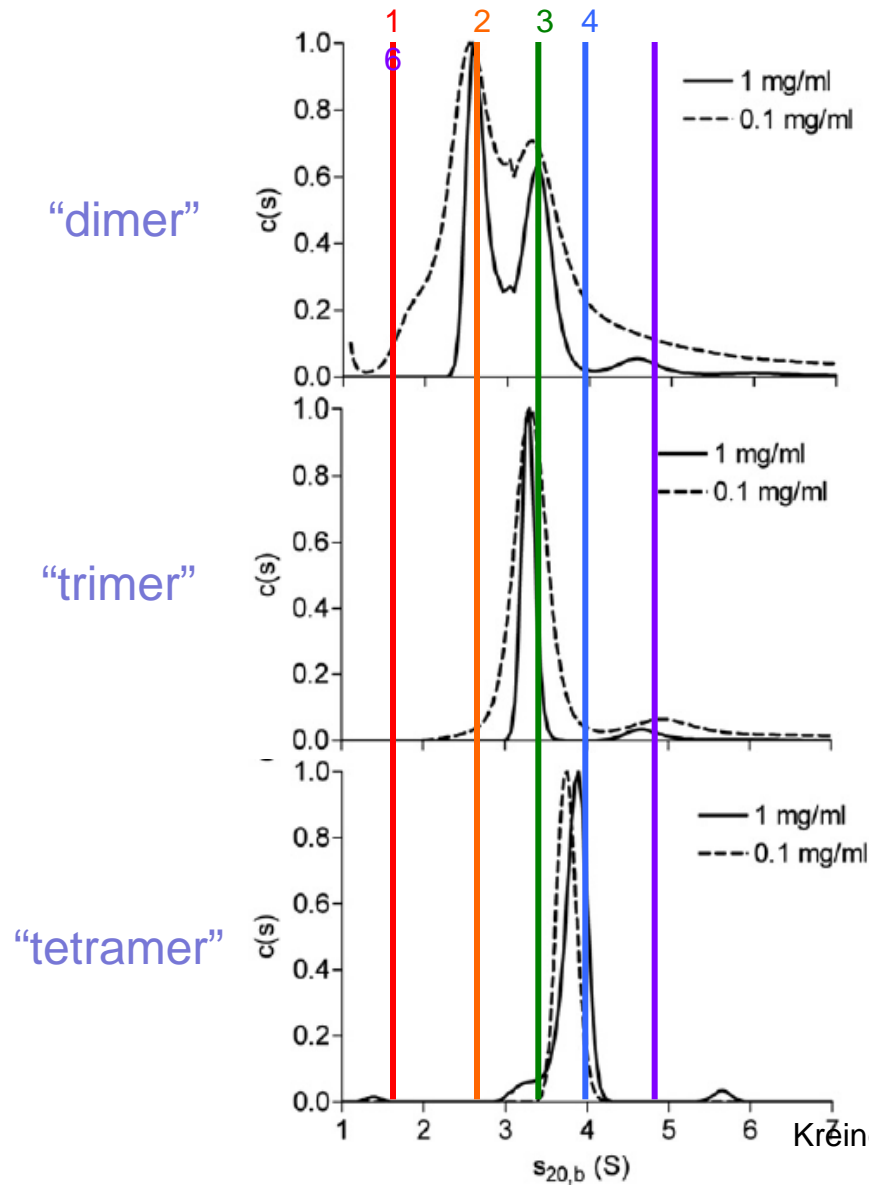
linear hexamer  
 $s = 5.0 S$  E



# AUC SV no DTT: c(s) analysis reveals complex composition



# AUC SV + DTT: $c(s)$ analysis reveals simplified composition



# Example: Oligomerisation of synthetic polyvalent integrin $\alpha_5\beta_1$ ligands

- $\alpha_5\beta_1$  ligands used to immobilise cells on surfaces via
  - 9th type III FN domain synergy site (PHSRN)
  - 10th type III FN domain RGD site
- $\alpha_5\beta_1$  ligand oligomers facilitate increased binding
- Oligomerisation accomplished via 5 heptad repeats based on GCN4 leucine zipper
  - I/L placed variously @ a and d positions to promote di-, tri- & tetramerisation
- Thiol-linked immobilisation to surface achieved via C-terminal Cys
  
- **Question: do the ligands oligomerise as designed?**
  - They do not!
  - AUC allows model-free observation of unexpected species
  - HMB allows interpretation of these species

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